

Model of a double-sided surface plasmon resonance fiber-optic sensor

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MOTIVATION

- To understand the polarization properties of a double-side deposited surface plasmon resonance (SPR) fiber-optic sensor [1, 2].
- To evaluate the influence of SPR layer geometry on the sensor performance.

SENSOR SETUP

PARAMETERS OF COMPUTATION

- Opt. fiber: NA = 0.22, $D = 200 \,\mu\text{m}$, $L = 1 \,\text{cm}$, fused silica core.
- Sensing layer: Au on a bare fiber core, $t_{\min} = 0$, $t_{\max} = 50 \text{ nm}$.
- The shape of layer outer boundary is approximated by an ellipse.
- Model analyte: aqueous solution of NaCl.

RESULTS

- Sensing structure is based on a step-index, multimode optical fiber.
- Interrogation in the wavelength domain is considered.
- Analysis carried out in frame of thin film optics.



- Fiber excited by a collimated/focused centered (CFC) beam.
- Input beam is linearly polarized.
- Double-side deposition of metal sensing SPR layer.

DOUBLE-SIDE GEOMETRY

• Double-side deposition leads to *inhomogeneous layer* \Rightarrow



Influence of φ on SPR spectra

- \triangleright The dip position is affected by φ .
- > The effect is higher for low c_{NaCl} - low refractive index of analyte.
- $\triangleright \text{ Increasing } \varphi \text{ leads to broad shallow} \\ \text{dips} \Rightarrow \text{detection ability decreases.}$
- ▷ For $\varphi > 47^{\circ}$ the detection is not possible for low c_{NaCl} .

Effect of layer geometry

- Double-side deposition leads to thickness change along the circumference of the core.
- The position of SPR resonance dip depends on film local thickness.
- $\triangleright \text{ The p-polarized component spectra} \\ I_{p} \text{ with different dip position are} \\ \text{summed} \Rightarrow \text{integration over polar} \\ \text{angle } \alpha \text{ leads to 'average' dip.} \end{cases}$



- layer thickness depends on polar angle: $t = t(\alpha), t \in \langle t_{\min}, t_{\max} \rangle$.
- The outer layer boundary approximated by an ellipse: semi-major axis: $a = t_{max} + \frac{D}{2}$, semi-minor: axis $a = t_{min} + \frac{D}{2}$.
- Because the layer thickness is much smaller than fiber core diameter *D* (low-eccentricity ellipse), skew rays in the layer are *omitted*.



- Input polarization azimuth given by φ (with respect to x-axis).
- Local decomposition of linear polarization to *p*-component (normal *n*) and *s*-component (tangent *t*) is needed.

POWER TRANSFER CALCULATION

• Polar angle dependence is considered \Rightarrow double integration.



 $\lambda ~ [
m nm]$

Dip shift with concentration

- $\triangleright \text{ For increasing } c_{\text{NaCl}} \text{ the dip position}$ is shifted to longer wavelength as the analyte refractive index increases.
- ▷ The increasing azimuth causes an opposite effect.
- $\triangleright The effect of azimuth orientation is more pronounced for low <math>c_{NaCl}$.

Sensitivity of the setup

- ▷ The sensitivity $S = \frac{\Delta \lambda_{dip}}{\Delta c_{mass}}$ increases with the analyte refractive index (increasing c_{NaCl}).
- The increase can be approximated by a linear function.
- ▷ The sensitivity increases with the



• Normalized power transfer spectrum on output of sensing part:

 $P_{\rm tn}(\lambda) = \frac{\int_{\alpha}^{2\pi} \int_{\theta_{\rm c}(\lambda)}^{\pi/2} \left[p^2(\varphi, \alpha) R_{\rm p}^N(\lambda, \theta) + s^2(\varphi, \alpha) R_{\rm s}(\lambda, \theta)^N \right] A(\theta) \, \mathrm{d}\theta \mathrm{d}\alpha}{\int_{\alpha}^{2\pi} \int_{\theta_{\rm c}(\lambda)}^{\pi/2} A(\theta) \, \mathrm{d}\theta \mathrm{d}\alpha}$

- Integration with respect to polar angle α and angle of incidence θ .
- $R_{\rm p,s}$ reflectances, $N_{\rm ref} = L/(D \tan \theta)$ number of reflections.
- Polarization projectors: $p = \frac{1}{\sqrt{2\pi}} \cos(\varphi \alpha), s = \frac{1}{\sqrt{2\pi}} \sin(\varphi \alpha).$
- Angular power distribution: $A(\theta) = \frac{n_1^2(\lambda) \sin \theta \cos \theta}{(1 n_1^2(\lambda) \cos^2 \theta)^2}$ (CFC beam).

input linear polarization azimuth.

REFERENCES

[1] Gonzalez-Cano, A. et all. Sensors 14, 4791-4805, (2014)
 [2] Nguyen Tan Tai et all. Opt. Express 22, 5590-5598, (2014)

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