# Model of a double-sided surface plasmon resonance fiber-optic sensor 

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## Motivation

- To understand the polarization properties of a double-side deposited surface plasmon resonance (SPR) fiber-optic sensor [1, 2].
- To evaluate the influence of SPR layer geometry on the sensor performance.


## SENSOR SETUP

- Sensing structure is based on a step-index, multimode optical fiber.
- Interrogation in the wavelength domain is considered.
- Analysis carried out in frame of thin film optics.

- Fiber excited by a collimated/focused centered (CFC) beam.
- Input beam is linearly polarized.
- Double-side deposition of metal sensing SPR layer.


## DOUBLE-SIDE GEOMETRY

- Double-side deposition leads to inhomogeneous layer $\Rightarrow$ layer thickness depends on polar angle: $t=t(\alpha), t \in\left\langle t_{\min }, t_{\max }\right\rangle$.
- The outer layer boundary approximated by an ellipse: semi-major axis: $a=t_{\max }+\frac{D}{2}$, semi-minor: axis $a=t_{\min }+\frac{D}{2}$.
- Because the layer thickness is much smaller than fiber core diameter $D$ (low-eccentricity ellipse), skew rays in the layer are omitted.

- Input polarization azimuth given by $\varphi$ (with respect to $x$-axis)
- Local decomposition of linear polarization to $p$-component (normal $\boldsymbol{n}$ ) and $s$-component (tangent $\boldsymbol{t}$ ) is needed.


## POWER TRANSFER CALCULATION

- Polar angle dependence is considered $\Rightarrow$ double integration.
- Normalized power transfer spectrum on output of sensing part:

$$
P_{\mathrm{tn}}(\lambda)=\frac{\int_{\alpha}^{2 \pi} \int_{\theta_{\mathrm{c}}(\lambda)}^{\pi / 2}\left[p^{2}(\varphi, \alpha) R_{\mathrm{p}}^{N}(\lambda, \theta)+s^{2}(\varphi, \alpha) R_{\mathrm{s}}(\lambda, \theta)^{N}\right] A(\theta) \mathrm{d} \theta \mathrm{~d} \alpha}{\int_{\alpha}^{2 \pi} \int_{\theta_{\mathrm{c}}(\lambda)}^{\pi / 2} A(\theta) \mathrm{d} \theta \mathrm{~d} \alpha}
$$

- Integration with respect to polar angle $\alpha$ and angle of incidence $\theta$.
- $R_{\mathrm{p}, \mathrm{s}}$ - reflectances, $N_{\text {ref }}=L /(D \tan \theta)$ - number of reflections.
- Polarization projectors: $p=\frac{1}{\sqrt{2 \pi}} \cos (\varphi-\alpha), s=\frac{1}{\sqrt{2 \pi}} \sin (\varphi-\alpha)$.
- Angular power distribution: $A(\theta)=\frac{n_{1}^{2}(\lambda) \sin \theta \cos \theta}{\left(1-n_{1}^{2}(\lambda) \cos ^{2} \theta\right)^{2}}$ (CFC beam).


## Parameters of computation

- Opt. fiber: $N A=0.22, D=200 \mu \mathrm{~m}, L=1 \mathrm{~cm}$, fused silica core.
- Sensing layer: Au on a bare fiber core, $t_{\min }=0, t_{\max }=50 \mathrm{~nm}$.
- The shape of layer outer boundary is approximated by an ellipse.
- Model analyte: aqueous solution of NaCl .


## Results



## Effect of layer geometry

$\triangleright$ Double-side deposition leads to thickness change along the circumference of the core.
$\triangleright$ The position of SPR resonance dip depends on film local thickness.
$\triangleright$ The p-polarized component spectra $I_{\mathrm{p}}$ with different dip position are summed $\Rightarrow$ integration over polar angle $\alpha$ leads to 'average' dip.

## Influence of $\varphi$ on SPR spectra

$\triangleright$ The dip position is affected by $\varphi$.
$\triangleright$ The effect is higher for low $c_{\mathrm{NaCl}}$ - low refractive index of analyte.
$\triangleright$ Increasing $\varphi$ leads to broad shallow dips $\Rightarrow$ detection ability decreases.
$\triangleright$ For $\varphi>47^{\circ}$ the detection is not possible for low $c_{\mathrm{NaCl}}$.


## Dip shift with concentration

$\triangleright$ For increasing $c_{\mathrm{NaCl}}$ the dip position is shifted to longer wavelength as the analyte refractive index increases.
$\triangleright$ The increasing azimuth causes an opposite effect.
$\triangleright$ The effect of azimuth orientation is more pronounced for low $c_{\mathrm{NaCl}}$.

## Sensitivity of the setup

$\triangleright$ The sensitivity $S=\frac{\Delta \lambda_{\text {dip }}}{\Delta c_{\text {mas }}}$ increases with the analyte refractive index (increasing $c_{\mathrm{NaCl}}$ ).
$\triangleright$ The increase can be approximated by a linear function.
$\triangleright$ The sensitivity increases with the input linear polarization azimuth.


## References

[1] Gonzalez-Cano, A. et all. Sensors 14, 4791-4805, (2014)
[2] Nguyen Tan Tai et all. Opt. Express 22, 5590-5598, (2014)

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