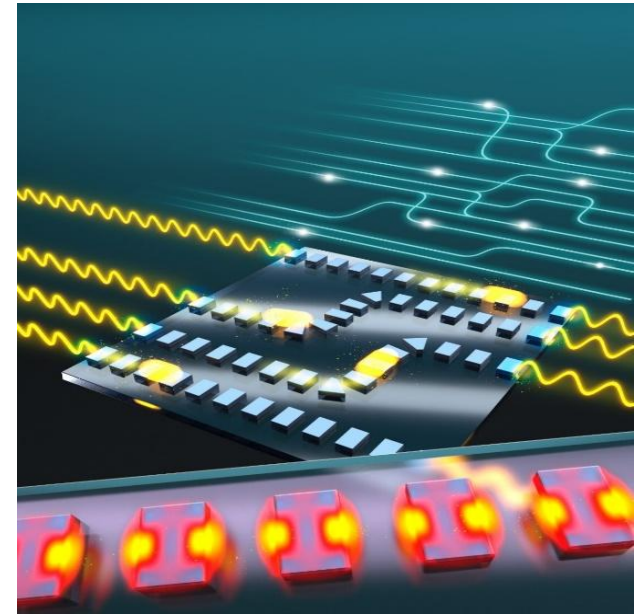
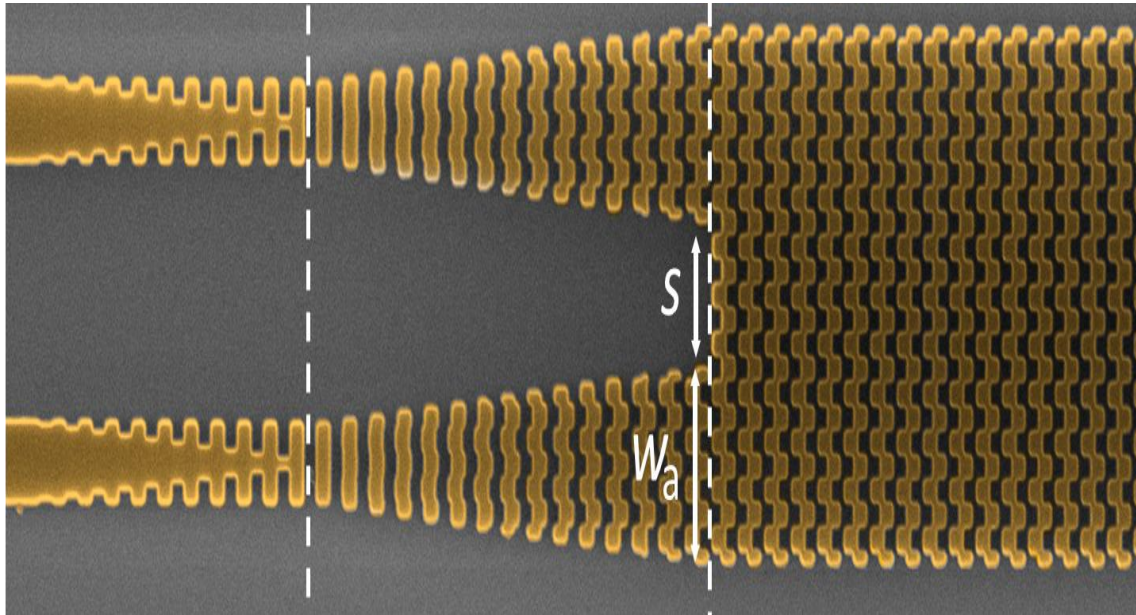




Metamaterial integrated photonics

Pavel Cheben

National Research Council Canada



**National Research Council,
Canada**

J.H. Schmid, J. Zhang, D.-X. Xu,
S. Janz, D. Melati, S. Wang,
M. Vachon, Y. Grinberg, R.
Cheriton, S. Bin-Alam, P. Cheben



Universidad de Málaga, Spain

R. Halir, G. Wangüemert-Pérez,
A. Ortega-Moñux, A. Sanchez
Postigo, I. Molina Fernandez, J.M.
Luque-González, D. Pereira-
Martín, A. Hadij Elhouati, P. Ginel
Moreno, A. F. Hinestrosa, A.
Sanchez Sanchez



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D. Benedikovic, M. Dado,
R. Korcek, J. Litvik



Universidad of Ottawa

P. Berini, S. Saeidi, T. Hao



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and CNRS, France**

C. Alonso-Ramos, D. Melati, D.
Marris Morini, D. Gonzales
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Czech Academy of Sciences

J. Ctyroky



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F. Setzpfandt, I. Staude



MADE ON EARTH

The humble mineral that transformed the world

BY DOUGLAS HEAVEN

Made On Earth

The story of the world's trading networks
told through eight everyday products.



Gordon Earle Moore (1929 – 2023)

The co-founder and emeritus chairman
of Intel Corporation.

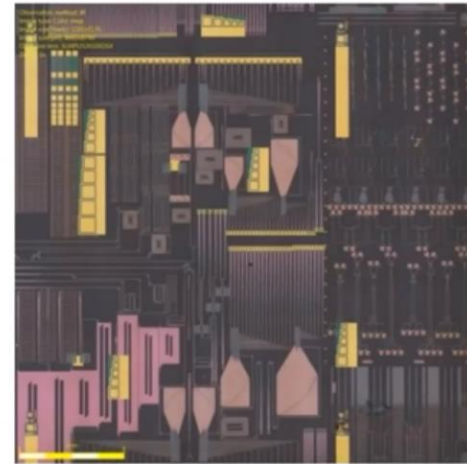
Silicon photonics

WHAT IS SILICON PHOTONICS?

The implementation of high density photonic integrated circuits by means of CMOS process technology in a CMOS fab



Pictures, courtesy of imec

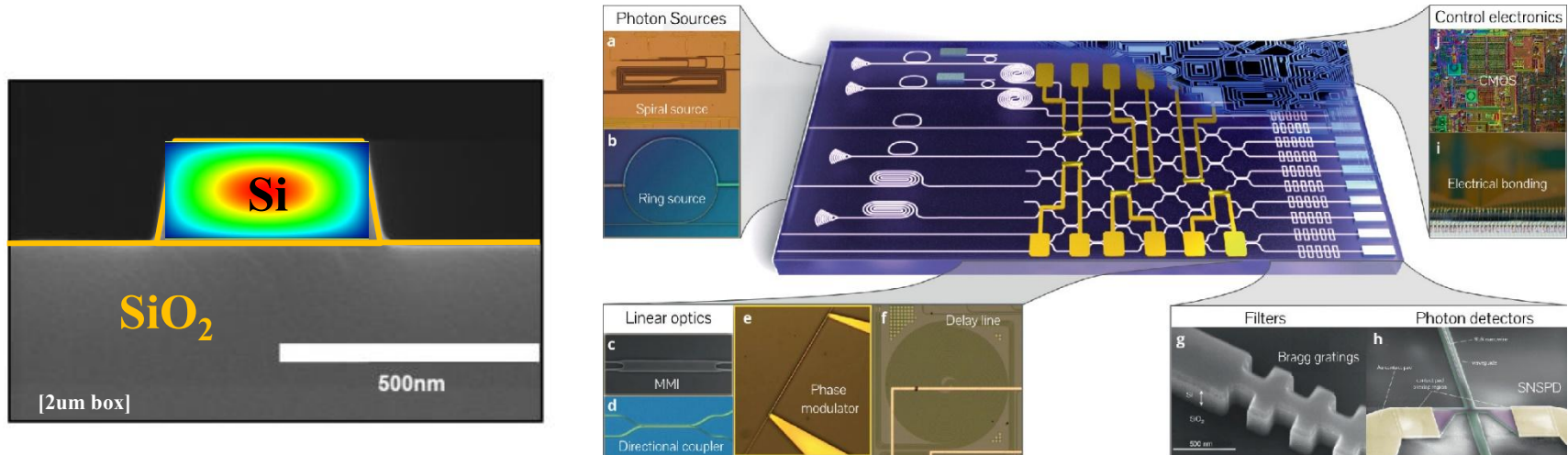


Enabling complex optical functionality on a compact chip at low cost

Courtesy Prof. Roel Baets

Silicon waveguides

- Starting from Silicon-on-Insulator wafers (SOI, from CMOS electronics), 200 mm or 300 mm
- Fabricated using 193 nm DUV or e-beam lithography and reactive ion etching (RIE).
- Standard waveguide: 450nm x 220nm
- Strongly confined mode (much smaller than in optical fibers)
- Bend radius $\sim 2 \mu\text{m}$

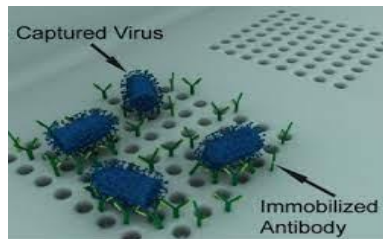


Silicon photonics

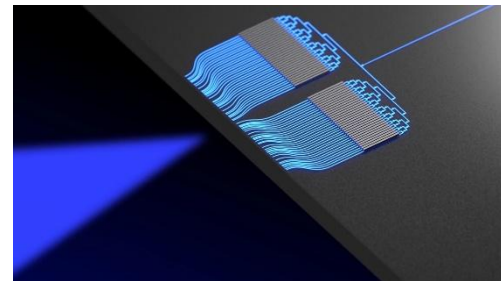
Telecom



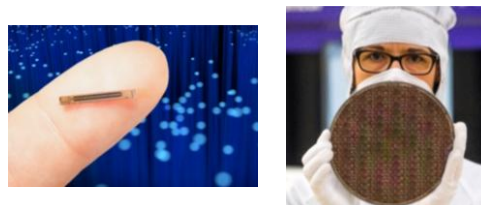
Sensing



Antenna phased arrays



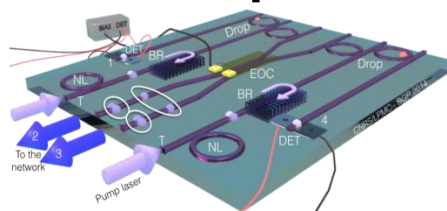
Datacom



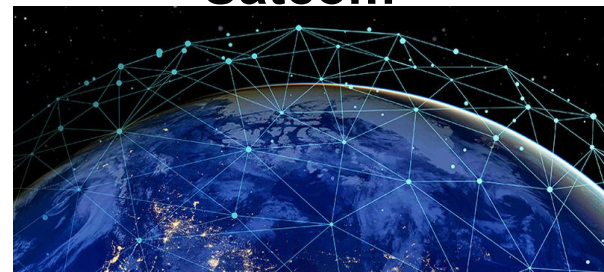
Lidars



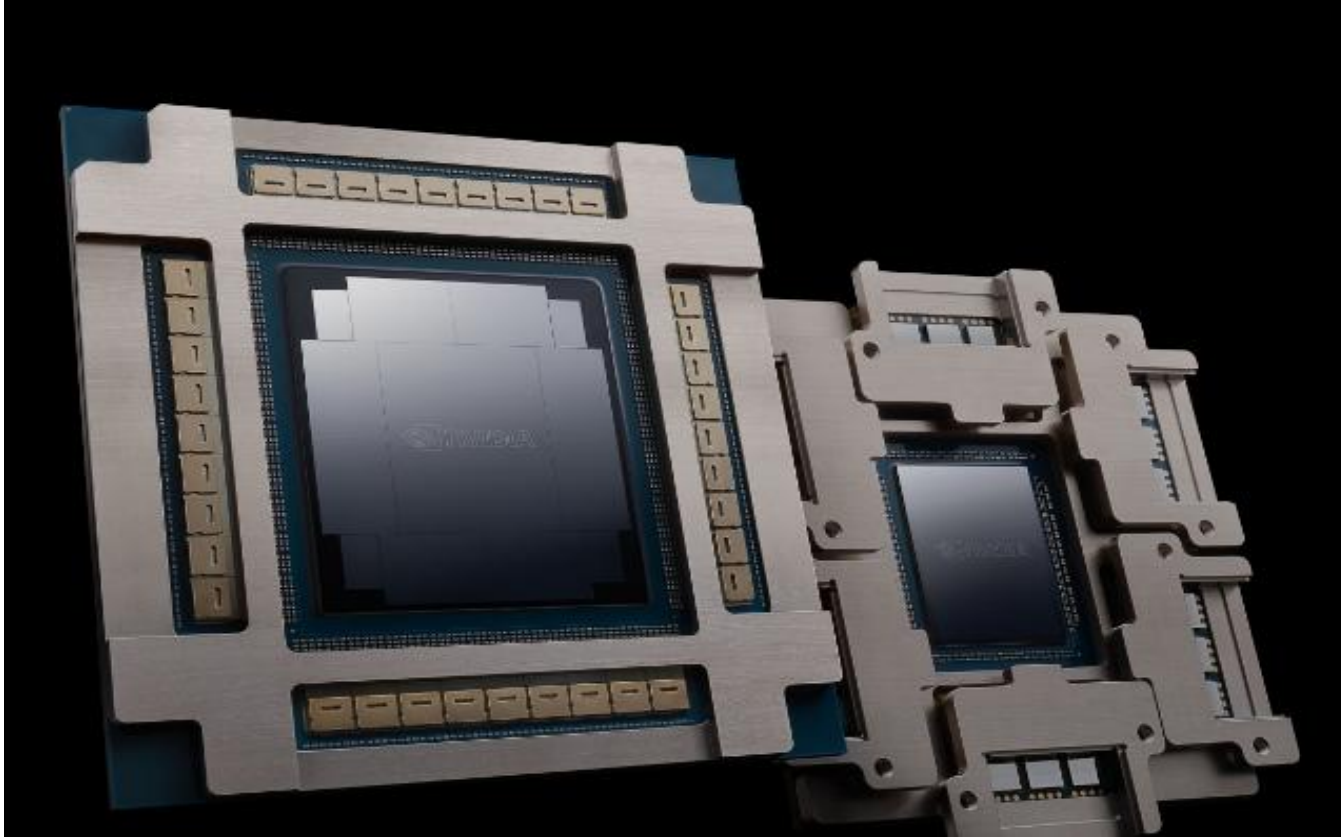
Quantum photonics



Satcom



NVIDIA Co-Packaged Silicon Photonic Networking Switch

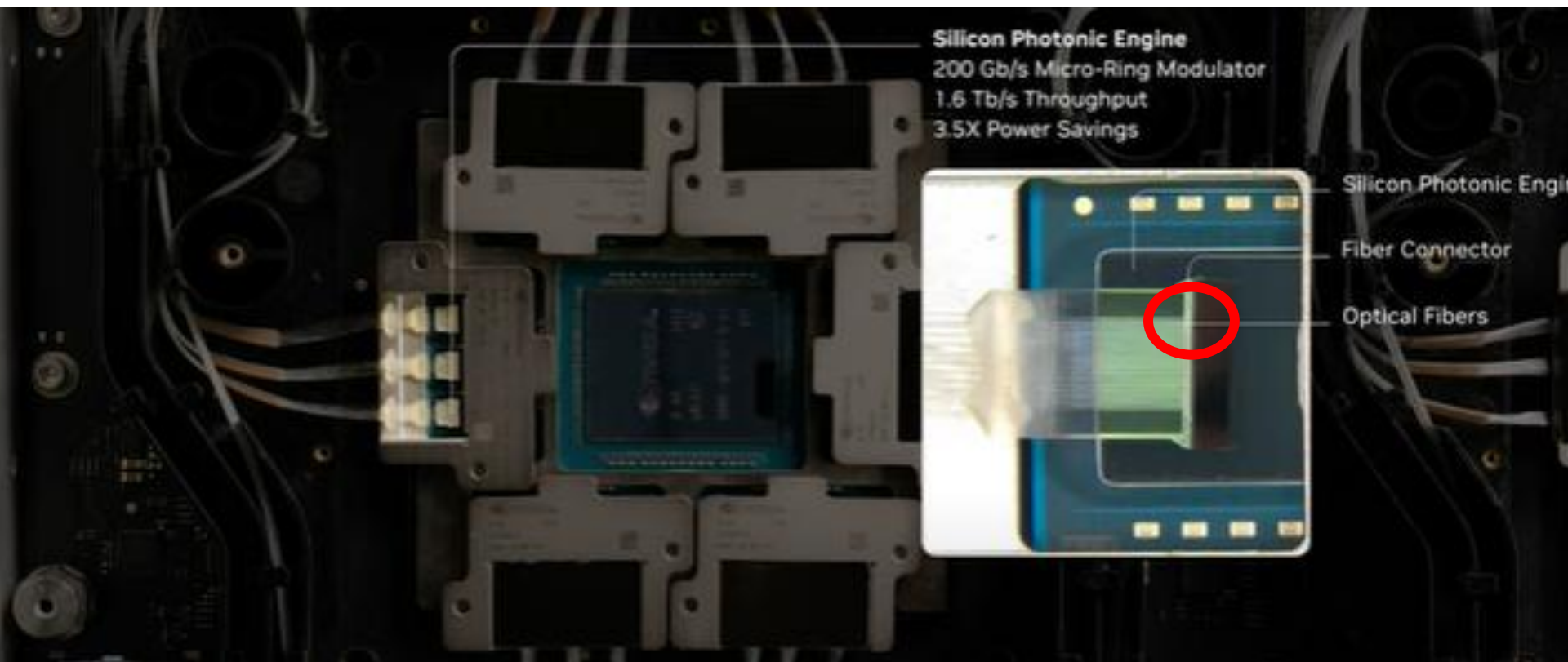


446 billion transistors

115 Tb/s throughput



324 Optical Connections
36 Laser Inputs
288 Data Links
Built-in Fiber Management



Silicon Photonic Engine
200 Gb/s Micro-Ring Modulator
1.6 Tb/s Throughput
3.5X Power Savings

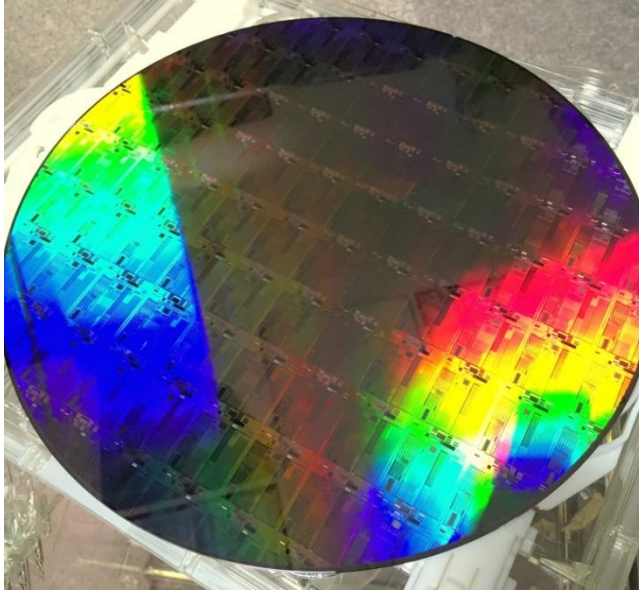
Silicon Photonic Engine
Fiber Connector
Optical Fibers



Multiplane data optical connectors
1152 Single mode fibers

The scale needed for the future million-GPU AI facilities

Silicon photonics design space challenge

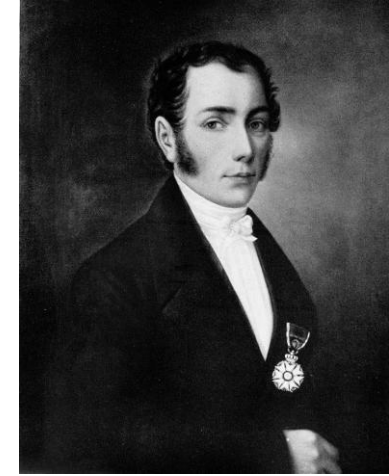
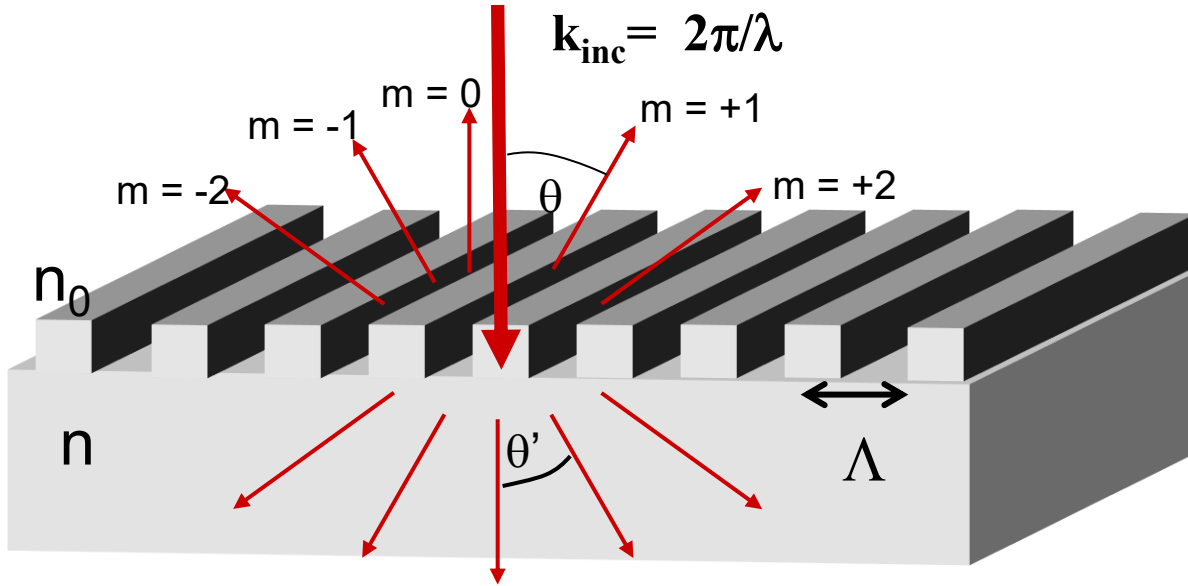


- Silicon fabrication provides two basic materials Si and SiO_2 (only two refractive indices $n=3.47$, $n=1.44$), unlike III-V semiconductor devices
- Adding new materials to the mix moves manufacturing outside traditional silicon fab capabilities

Can the silicon design space be expanded without losing the advantages and simplicity of silicon?

Subwavelength optics

Diffraction grating



Joseph Ritter von Fraunhofer
*1787, †1826

Grating equation (normal incidence):

$$\sin \theta = \frac{m\lambda}{\Lambda} \quad n \sin \theta' = \frac{m\lambda}{\Lambda}$$

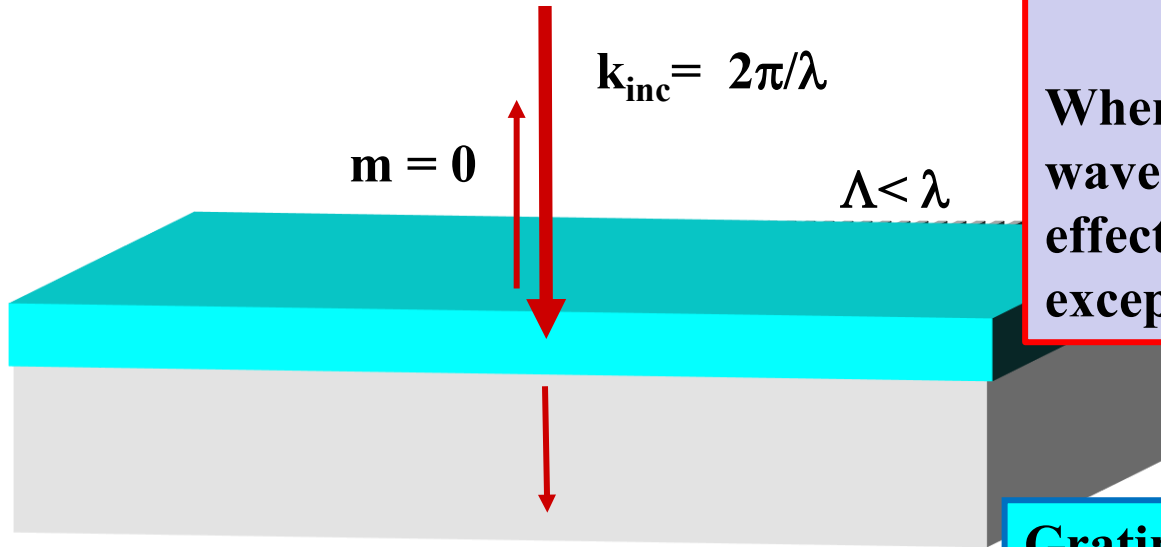
(backward)

(forward)

Diffraction grating:

$$\Lambda > \lambda \quad \text{and} \quad m < \frac{\Lambda}{\lambda}$$

Subwavelength grating



Subwavelength grating:

$$\Lambda < \lambda \rightarrow m\lambda / \Lambda > 1$$

$$\sin \theta = \frac{m\lambda}{\Lambda}$$

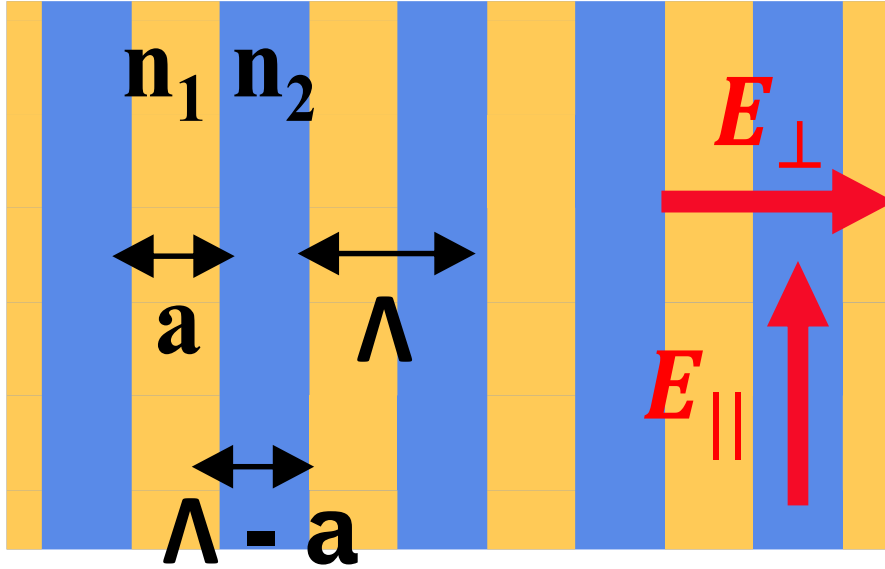
$$n \sin \theta' = \frac{m\lambda}{\Lambda}$$

NO DIFFRACTION

When grating period Λ is less than wavelength of light λ , diffraction effects are suppressed for all orders except $m = 0$.

Grating region behaves like a homogeneous anisotropic layer with an equivalent dielectric permittivity tensor.

Rytov's formulas

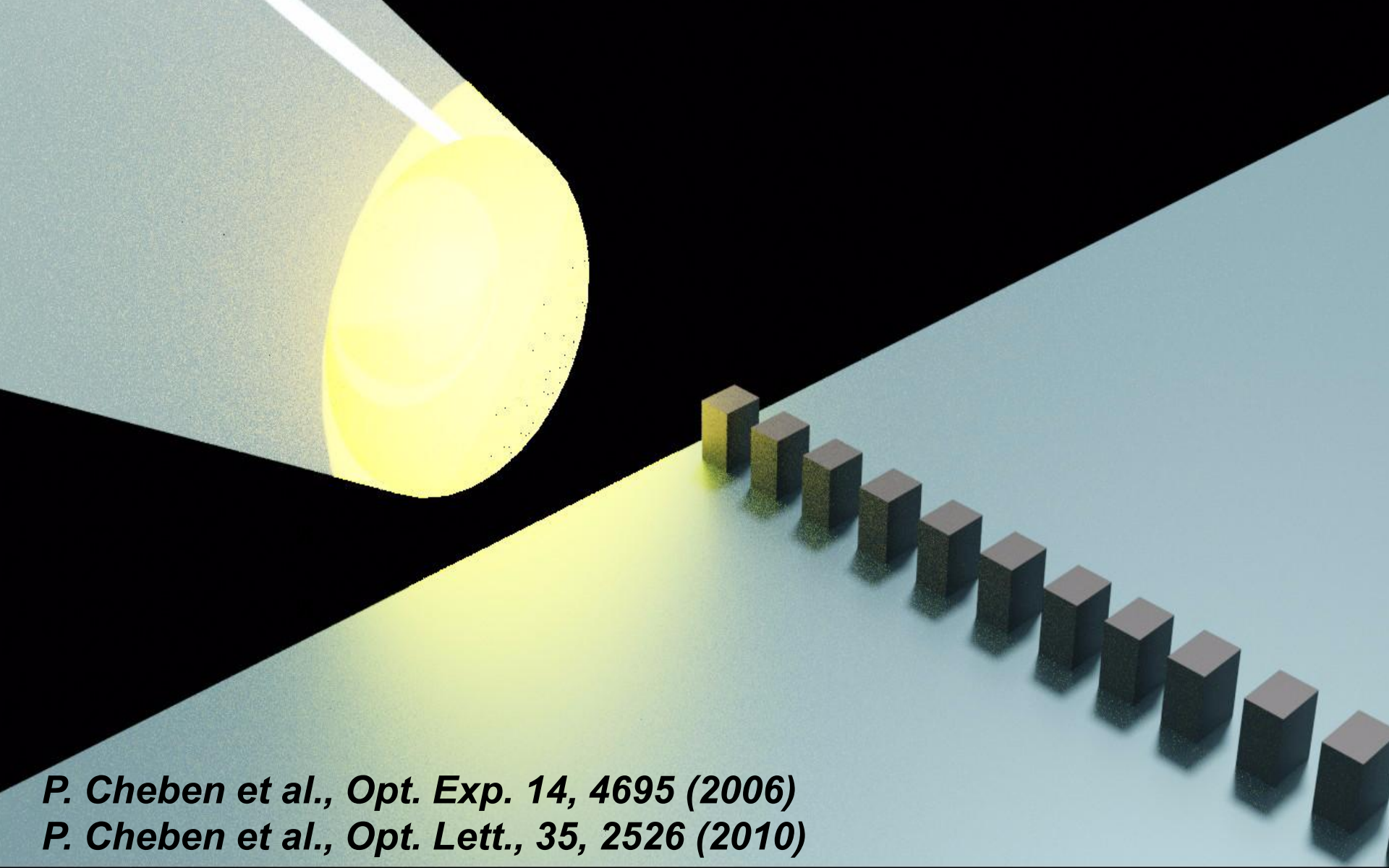


$$n_{\parallel}^2 = \frac{a}{\Lambda} n_1^2 + \left(1 - \frac{a}{\Lambda}\right) n_2^2$$
$$\frac{1}{n_{\perp}^2} = \frac{a}{\Lambda} \frac{1}{n_1^2} + \left(1 - \frac{a}{\Lambda}\right) \frac{1}{n_2^2}$$



S. M. Rytov, Soviet Phys. JETP 2, 466-475 (1956)

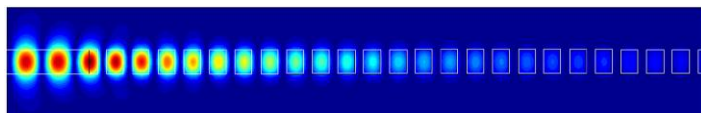
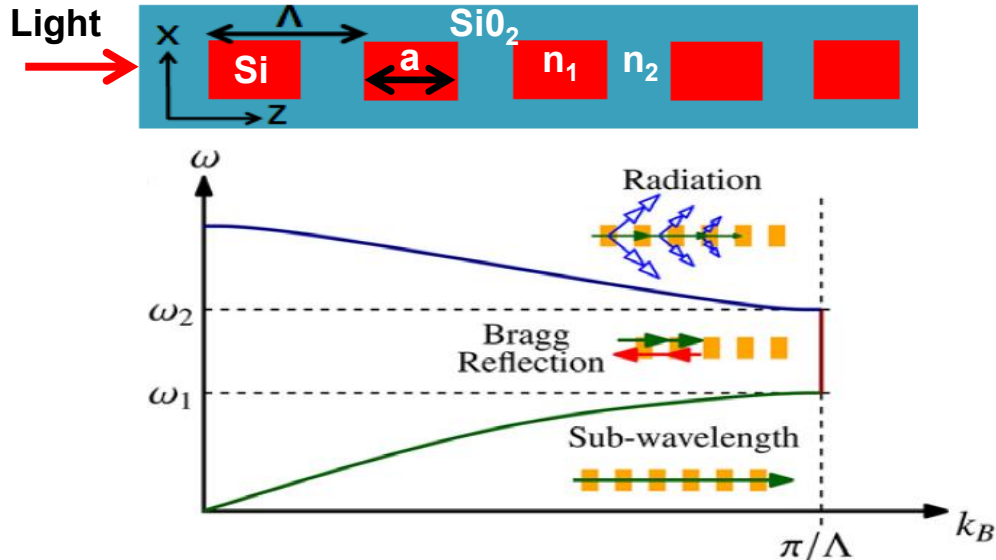
Sergei Mikhailovich Rytov (1908 –1996), a Soviet physicist.



P. Cheben et al., Opt. Exp. 14, 4695 (2006)

P. Cheben et al., Opt. Lett., 35, 2526 (2010)

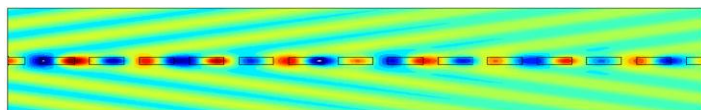
Periodic waveguides



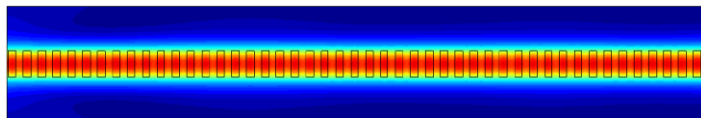
$\Lambda \sim \lambda_{\text{eff}}/2$: Bragg gratings, photon. crystals

Ken Hill, CRC Canada, 1976

Eli Yablonovitch and Sajeev John, 1987



$\Lambda > \lambda_{\text{eff}}/2$: Radiative gratings



$\Lambda < \lambda_{\text{eff}}/2$: SWG waveguides

NRC Canada, 2006

Floquet-Bloch mode in a periodic waveguide

$$\frac{d^2\psi(z)}{dz^2} + P(z)\psi(z) = 0$$

(Gaston Floquet, 1883)

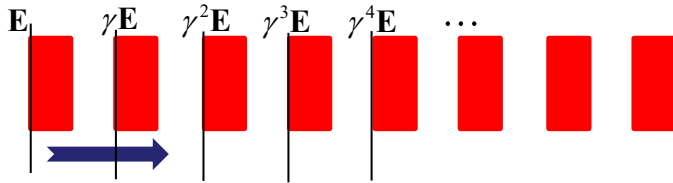
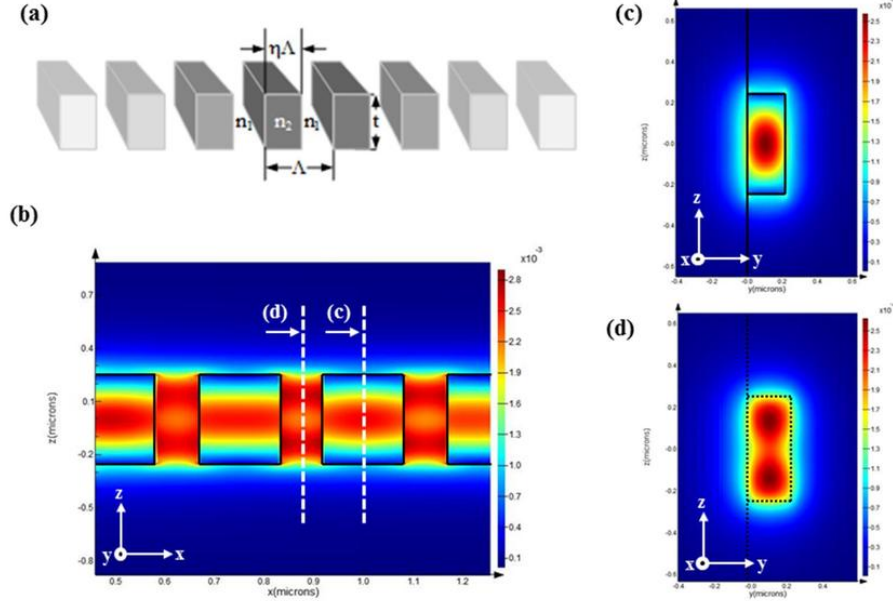
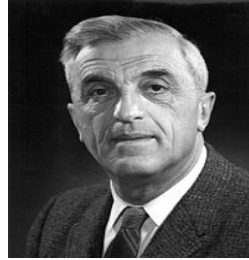
Second-order differential equation with periodic coefficients, $P(z \pm \Lambda) = P(z)$

Felix Bloch

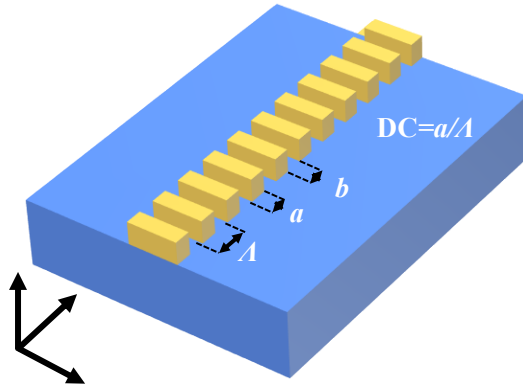
Solution is a periodic function:

$$\psi(z) = e^{ikz}u(z)$$

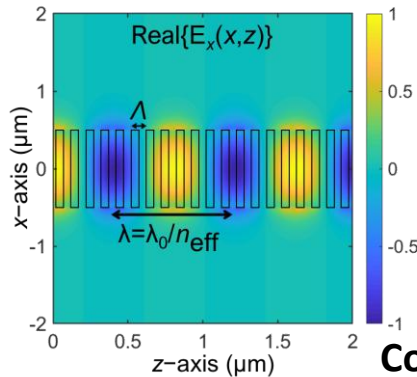
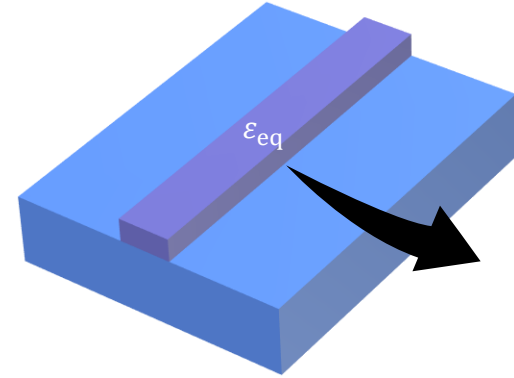
Where $u(z \pm \Lambda) = u(z)$



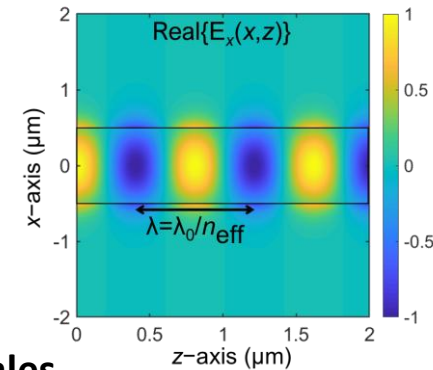
SWG metamaterial waveguide



$$\Lambda \ll \lambda$$

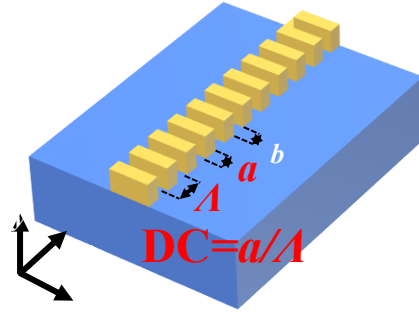


Courtesy - Jose Manuel Luque-Gonzales



Waveguide core equivalent refractive index controlled by “mixing” two dielectric materials by varying grating geometry

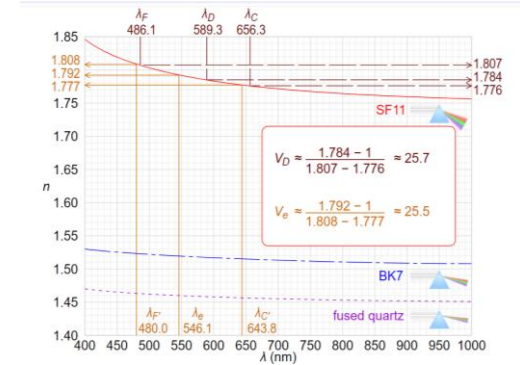
Engineering waveguide properties



Ernst Abbe



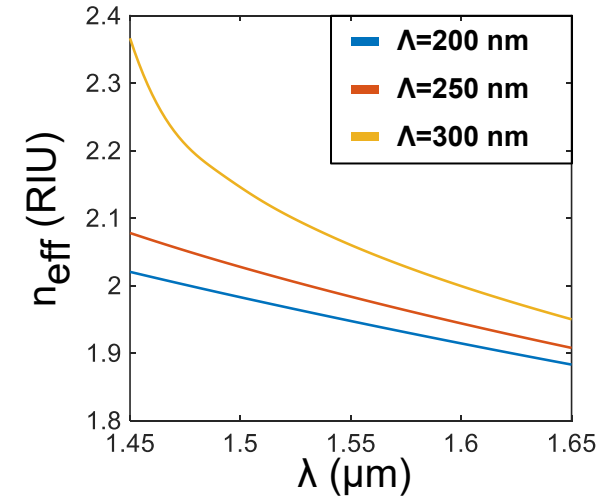
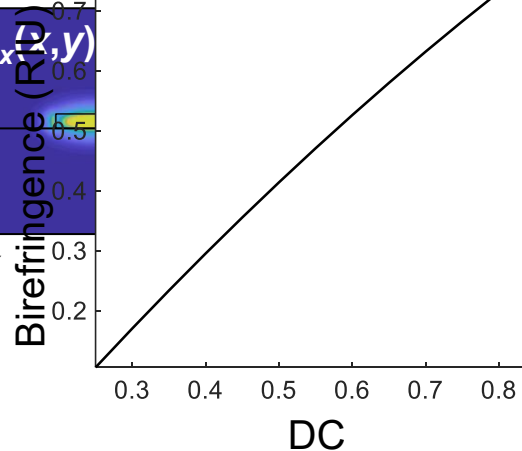
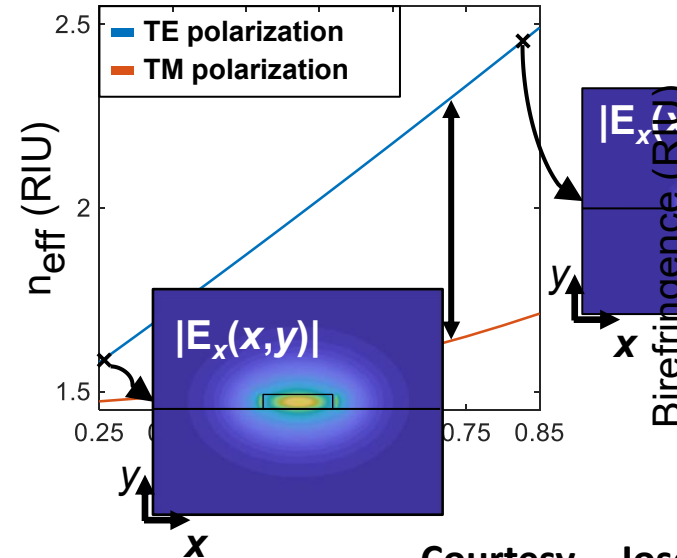
$$V_d \equiv \frac{n_d - 1}{n_F - n_C}$$



Refractive index engineering

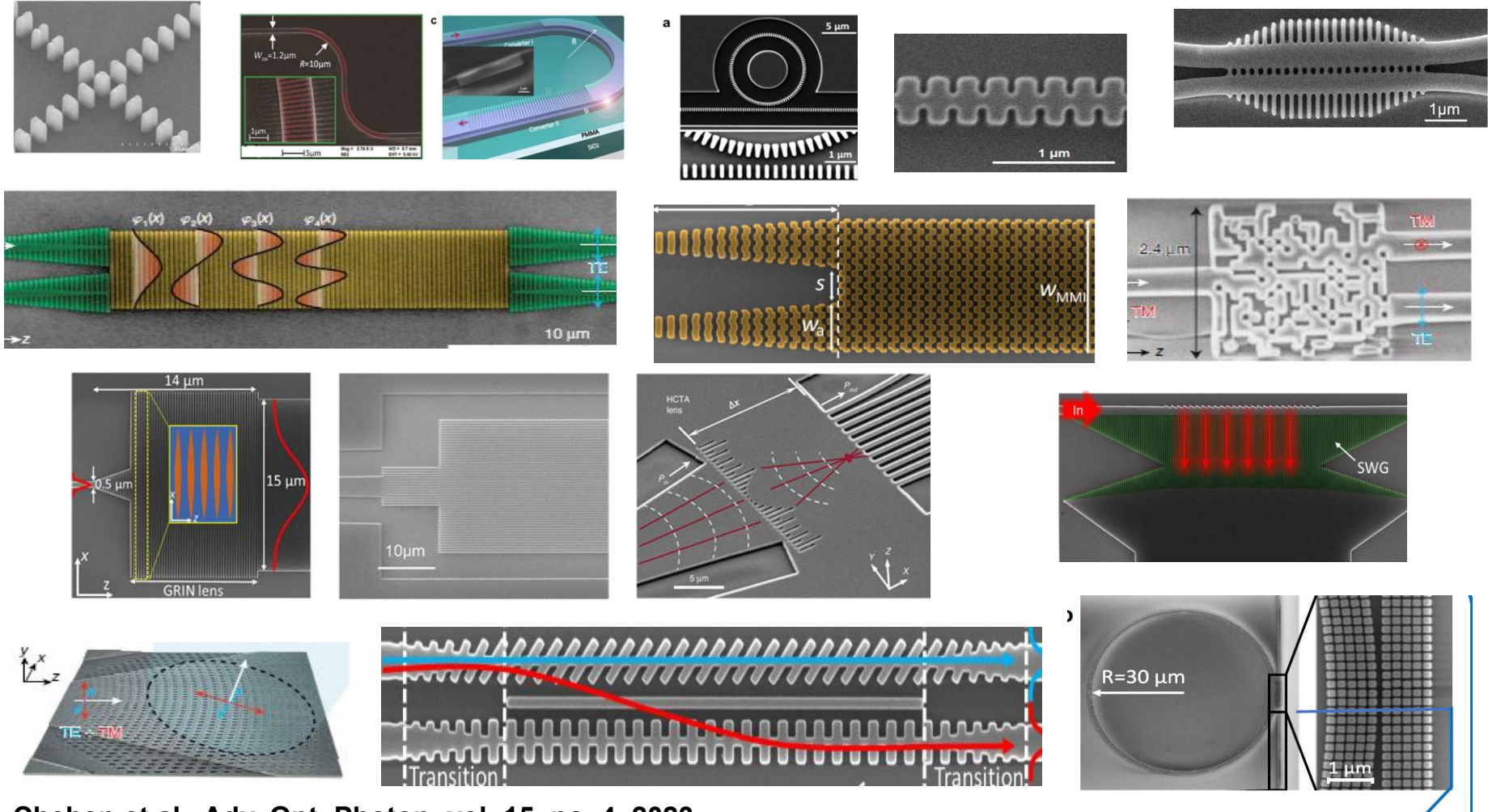
Birefringence/Anisotropy engineering

Dispersion engineering



Courtesy - Jose Manuel Luque-Gonzales

Surging field of research

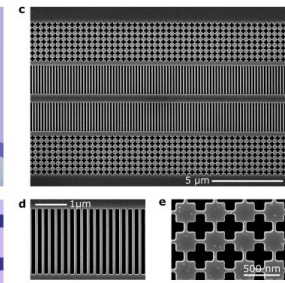
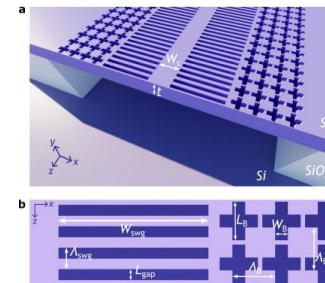
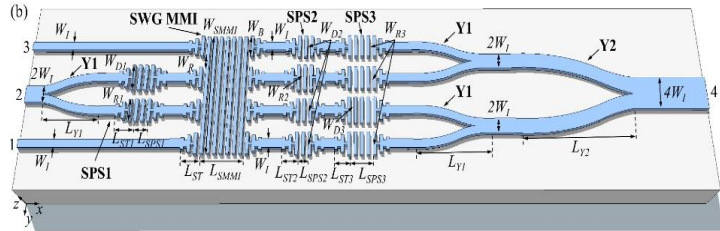
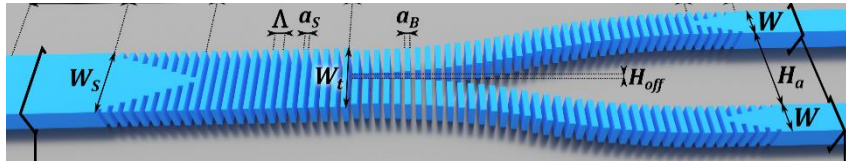
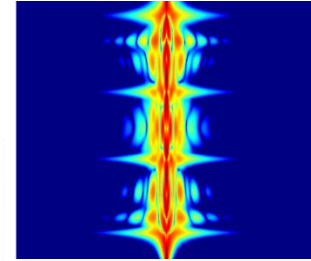
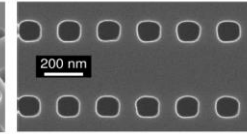
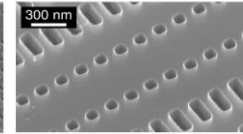
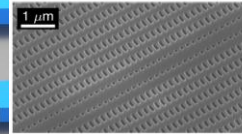
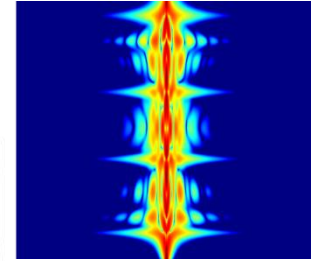
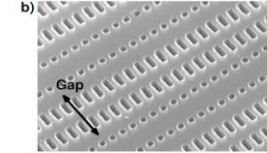
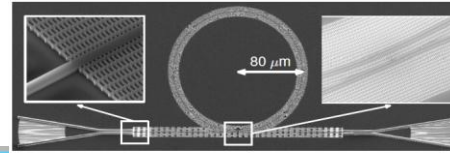
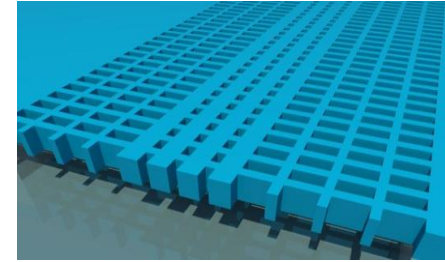
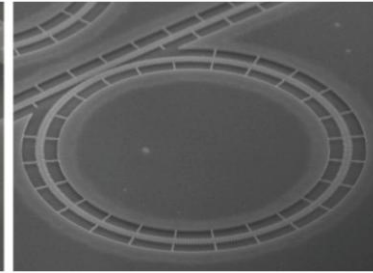
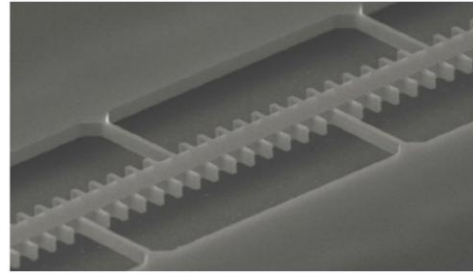
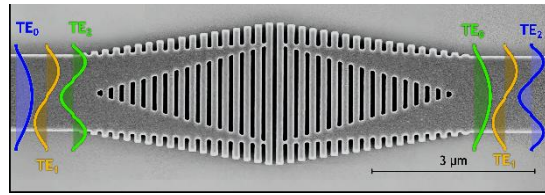
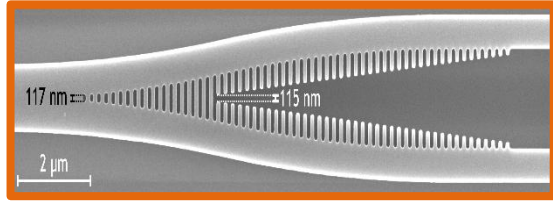


P. Cheben et al., Adv. Opt. Photon, vol. 15, no. 4, 2023

P. Cheben et al., Nature, vol. 560, no. 7720, 2018

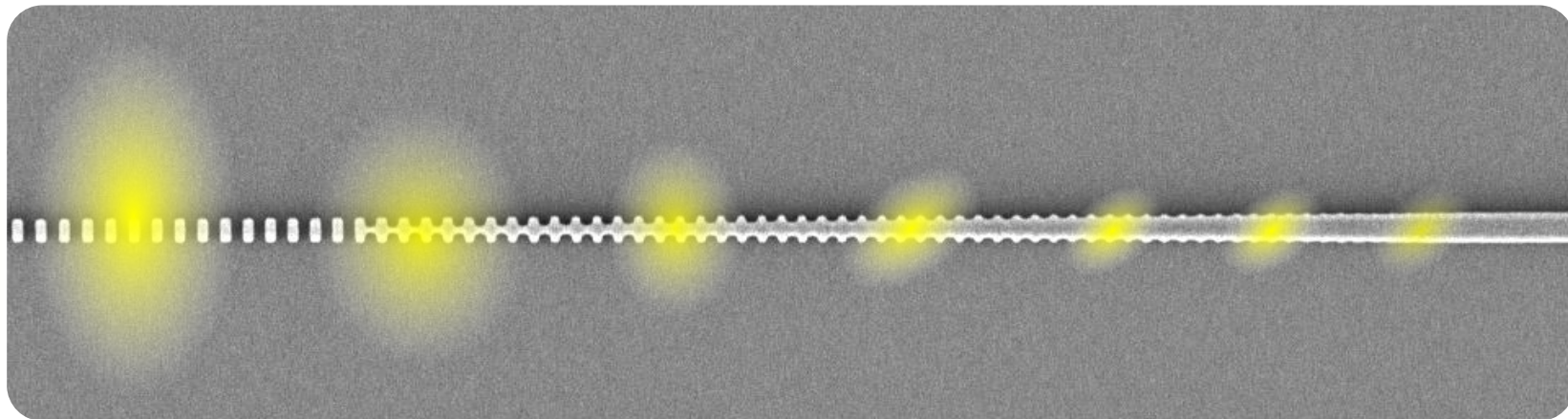
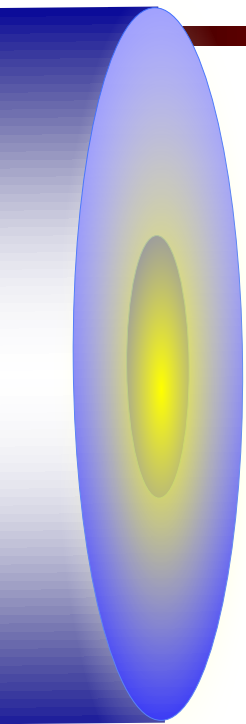
Halir et al., Proceedings of the IEEE, vol. 106, no. 12, 2018

Surging field of research



- P. Cheben et al., Adv. Opt. Photon, vol. 15, no. 4, 2023
 P. Cheben et al., Nature, vol. 560, no. 7720, 2018
 R. Halir et al., Proceedings of the IEEE, vol. 106, no. 12, 2018

SWG metamaterial fiber-chip coupler



P. Cheben et al., US Patent 7,680,371

P. Cheben et al., Opt. Express, vol. 14, p. 4695 (2006)

P. Cheben et al., Opt. Lett., vol. 35, p. 2526 (2010)

P. Cheben et al., Opt. Express, vol. 23, p. 22554 (2015)

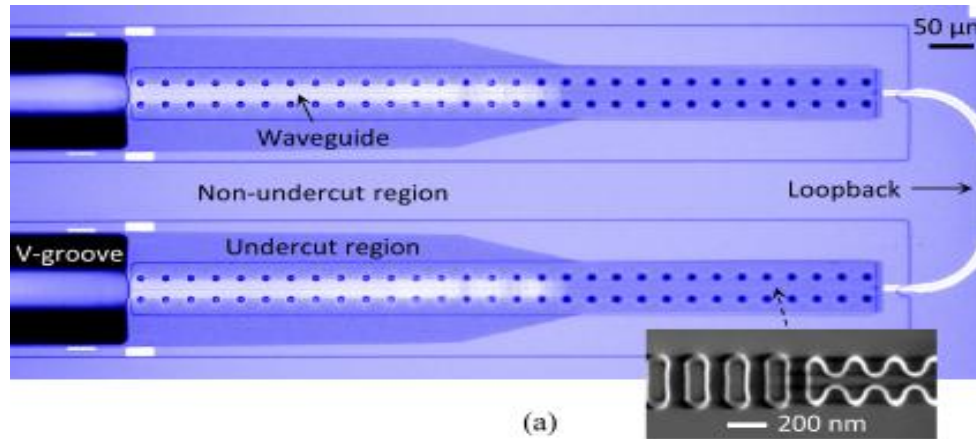
Loss 0.32dB (93%), BW > 100nm

PDL<0.05dB, MFD=3.2 μ m

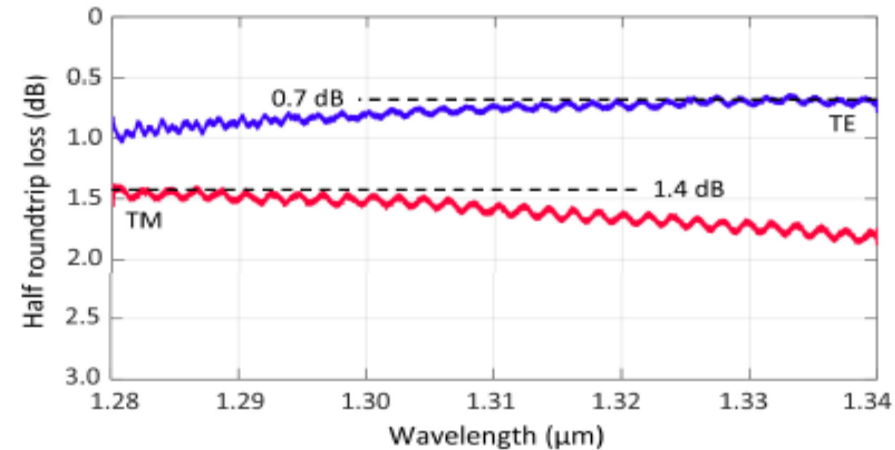
NRC with Teraxion, Ciena

Minimum feature size 100 nm
E-beam, but compatible with deep-up

IBM metamaterial coupler



T. Barwicz et al., OFC 2015, Paper Th3F
T. Barwicz et al., OFC 2016, Paper M2I.3
T. Barwicz et al., OFC 2017, Paper Th2A.39

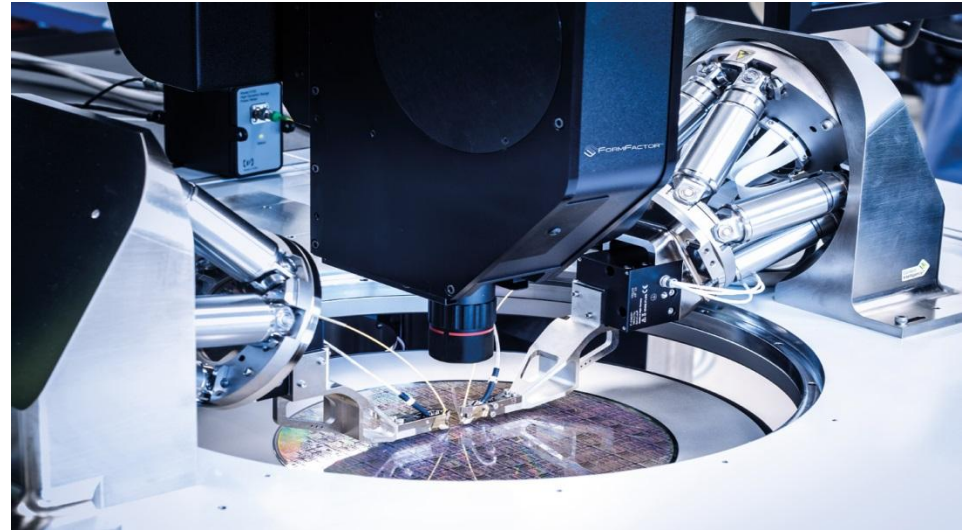
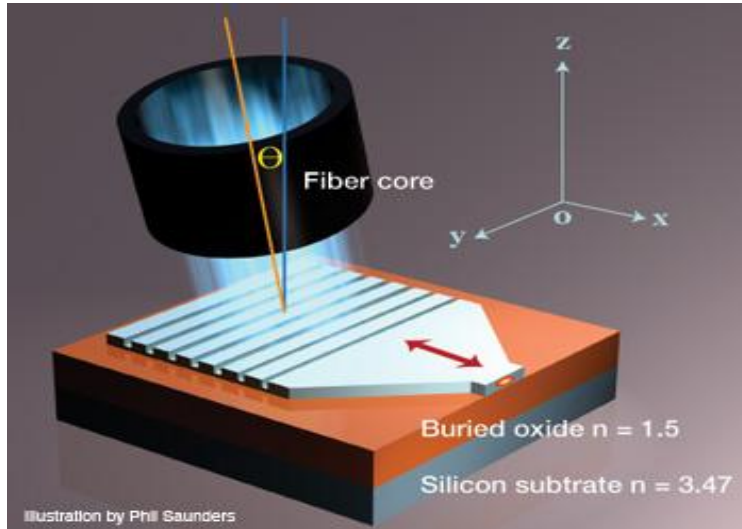


- 0.7 dB transmission loss from SMF-28 optical fiber to Si waveguide
- Localized substrate removal for large mode size
- Reflection -36 dB (TE) and -43 dB (TM)
- Available through a commercial product design kit

T. Barwicz et al., IEEE JSTQE, Vol. 25, No. 3 (2019)



Surface grating couplers



High-throughput optical probing of on-wafer silicon photonic devices (Formfactor)

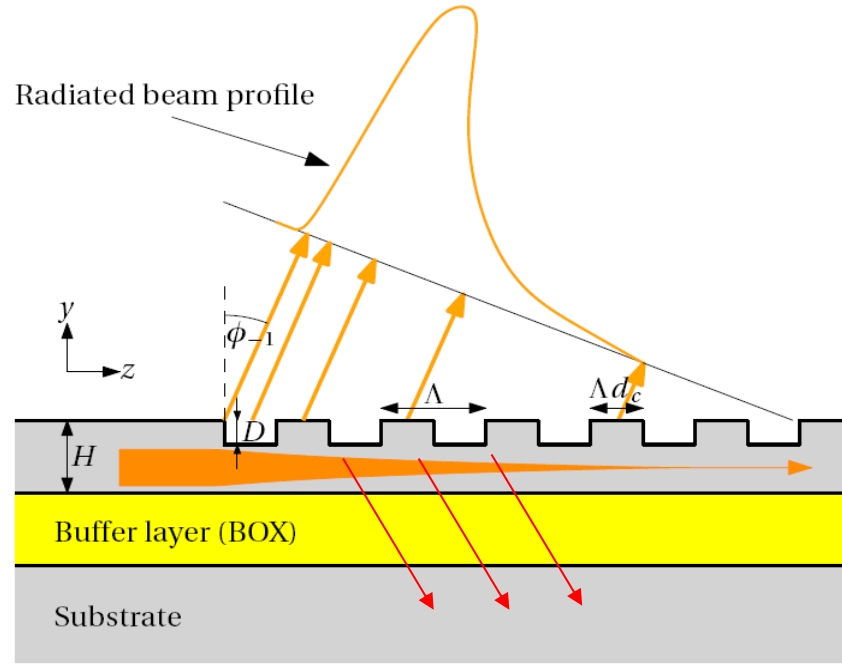
Pros:

- Easier alignment
- No facet preparation
- Wafer level testing

Cons:

- Achieving sub-1dB efficiency is a challenge
- Limited wavelength range

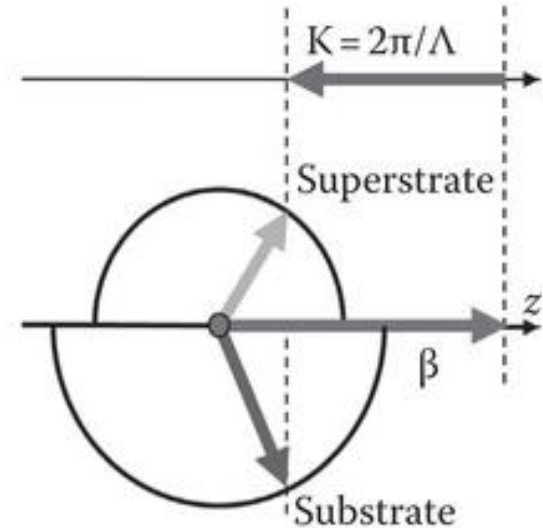
Surface grating couplers



$$k_0 n_{\text{eff}} = k_0 n_c \sin \phi + mK$$

$$k_0 = 2\pi/\lambda_0$$

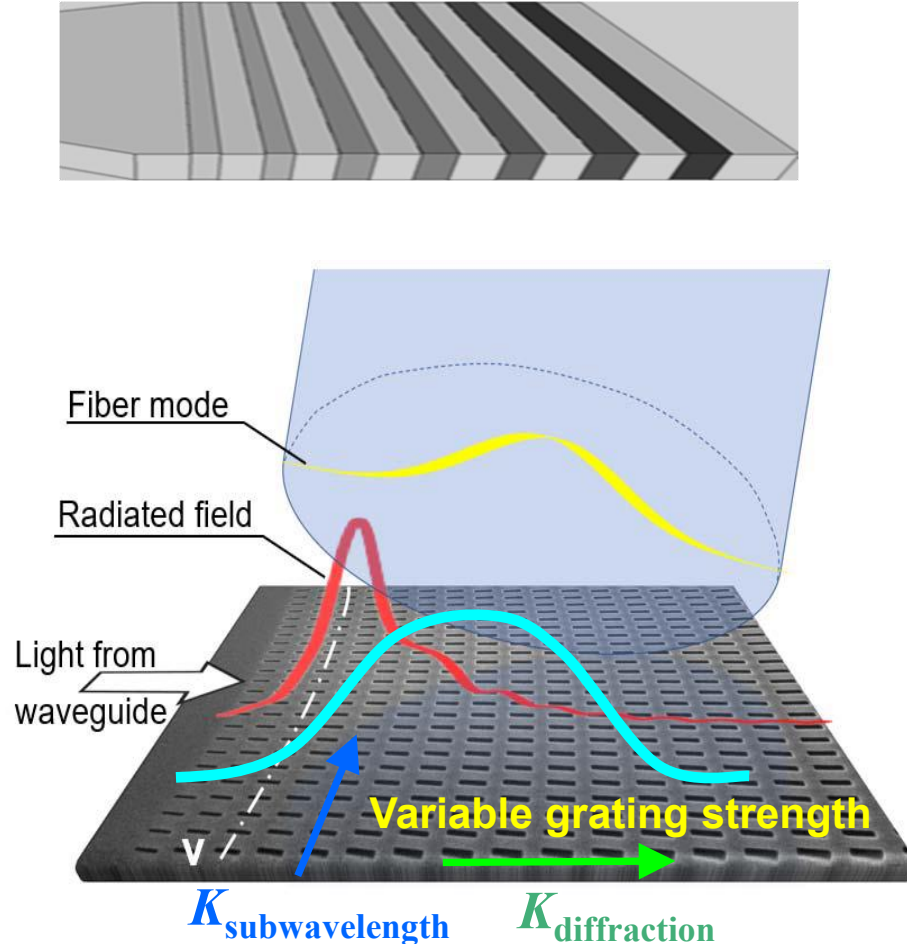
$$K = 2\pi/\Lambda$$



- Exponential near field, max. 80% overlap with a Gaussian beam (SMF-28)
- For field matching with an optical fiber, grating apodization is required
- Radiation loss to substrate

SWG surface grating couplers

Apodized grating



- Diffractive grating along longitudinal direction
- Non-diffractive SWG along transverse direction emulates shallow etch / apodization
- Surface grating strength can be defined and continuously varied across chip
- Apodization in one lithography / etch step along with waveguide.

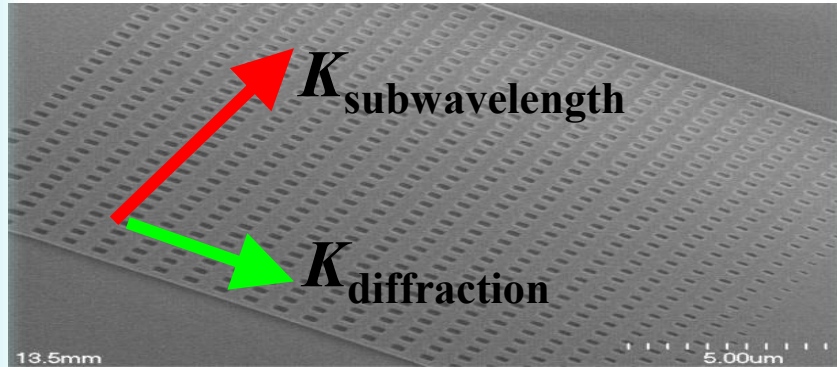
R. Halir et al., Opt. Lett., 34, 1408, 2009

X. Chen et al., IEEE Photon. J. 1, 184, 2009

R. Halir et al., Opt. Lett., 35, 3243, 2010

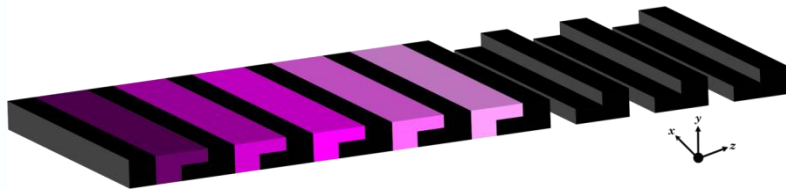
High-efficiency grating couplers

E-beam



D. Benedikovic *et al.*, Opt. Expr. 23 (2015)

-0.7 dB (experiment)

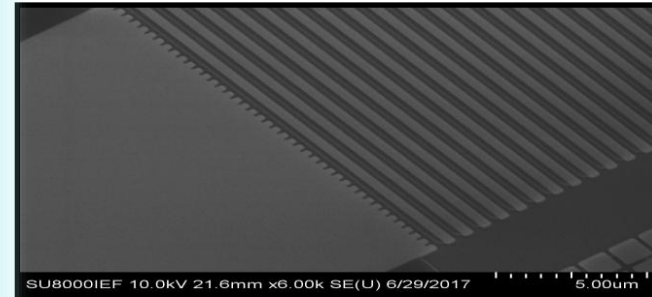


D. Benedikovic *et al.*, Opt. Expr. 2019

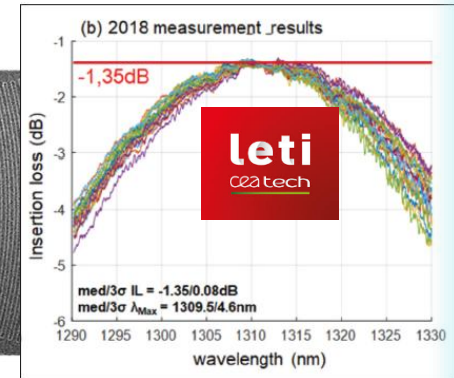
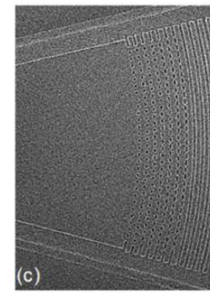
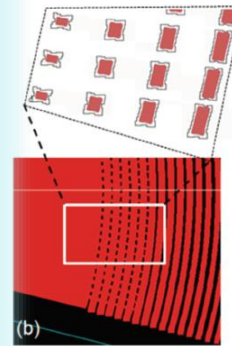
-0.25 dB (3D FDTD)



Deep-uv



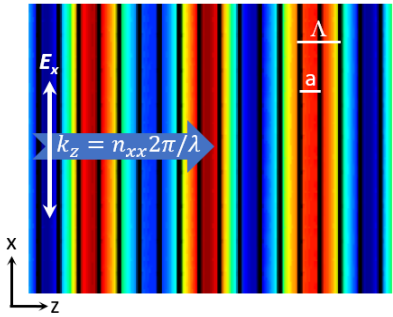
D. Benedikovic *et al.*, Opt. Letters 42 (2017)



D. Fowler *et al.*, CEA LETI (2018)

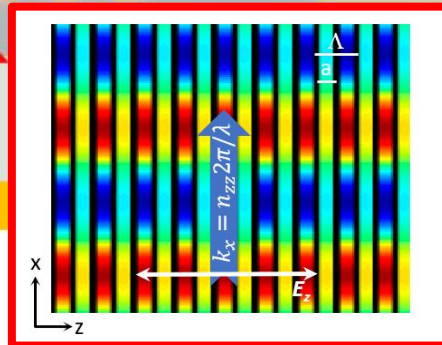
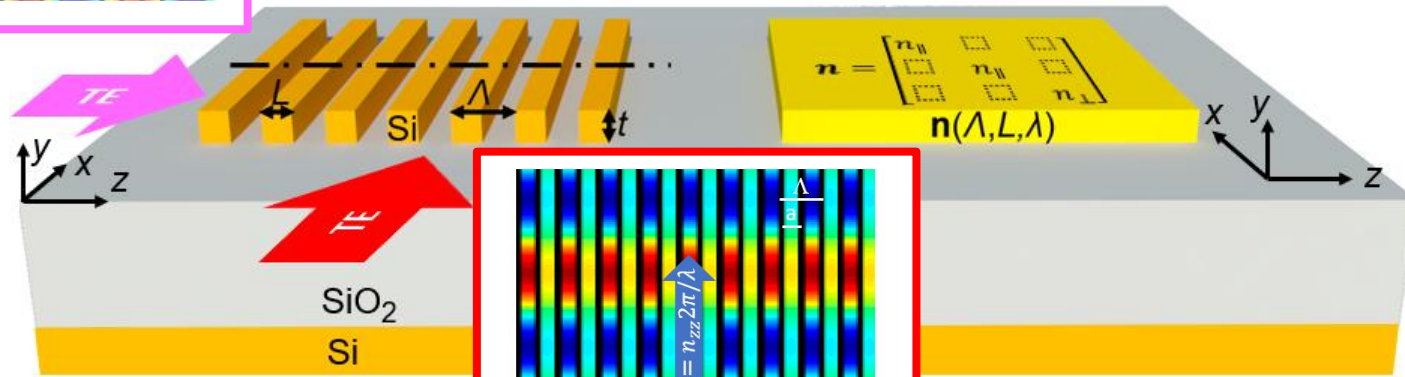
-1.35 dB (experiment)

Engineering waveguide anisotropy



$$n_{\parallel}^2 \approx \frac{L}{\Lambda} n_{Si}^2 + \left(1 - \frac{L}{\Lambda}\right) n_{SiO_2}^2$$

S. M. Rytov, Sov. Phys. JETP 2, 1956

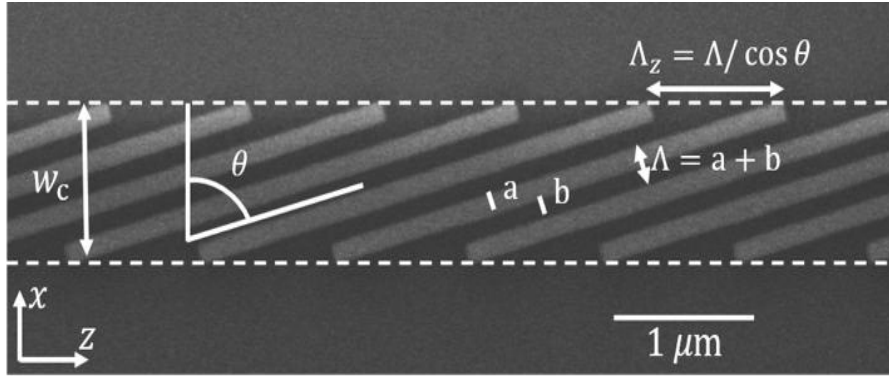


$$n_{\perp}^{-2} \approx \frac{L}{\Lambda} n_{Si}^{-2} + \left(1 - \frac{L}{\Lambda}\right) n_{SiO_2}^{-2}$$

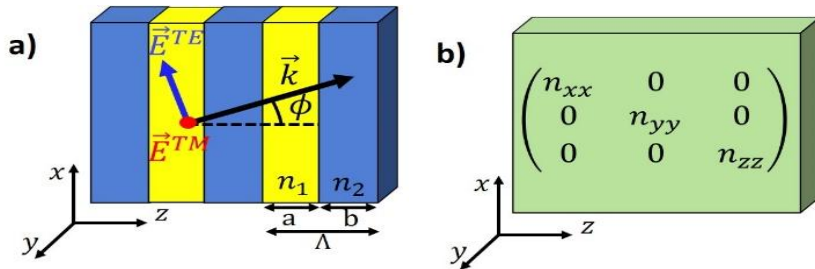
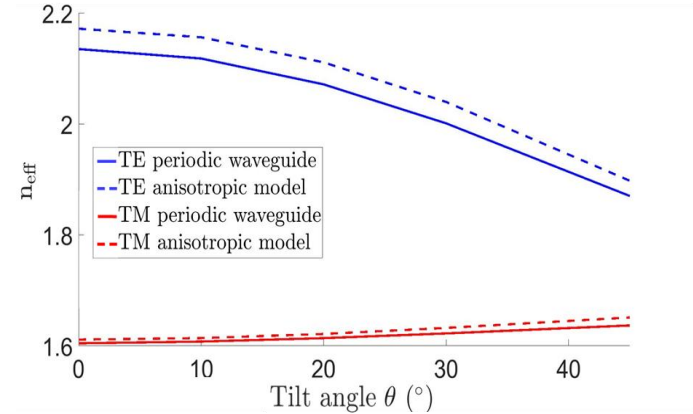
Courtesy: Robert Halir, UMalaga

Luque-González et al., Optics Letters 43, 2018

Controlling anisotropy of Si-wires

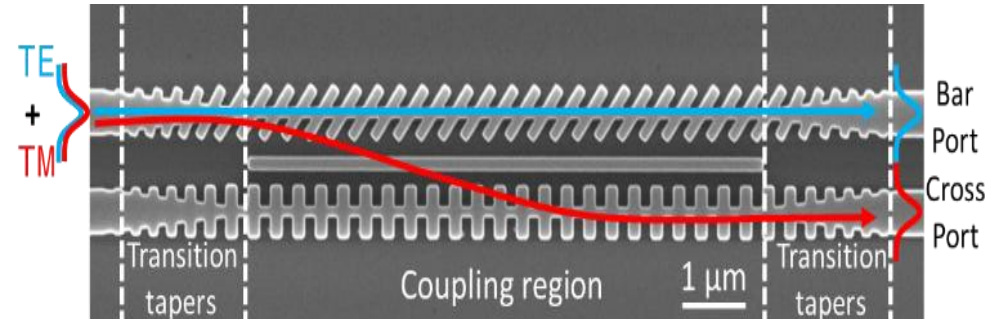


Tilted SWG waveguide. $w_c = 1\mu\text{m}$, $\Lambda = 0.25\mu\text{m}$, $DC = 0.5$, $\theta = 75^\circ$. The SWG period $\Lambda_z = \Lambda / \cos(\theta)$.



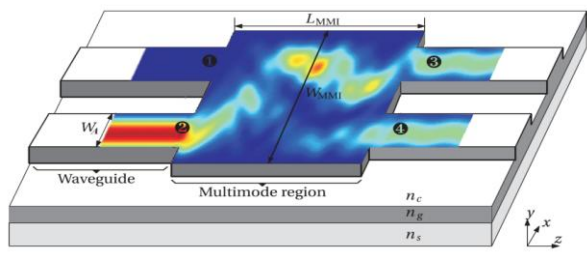
J. M. Luque-González et al., Opt. Lett.
vol. 43, 4691 (2018)

Polarization splitter



J. M. Luque-González et al., Optics Letters (2020)

Ultra-broadband MMI coupler



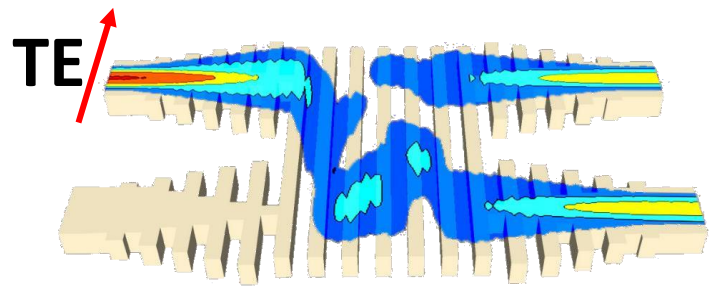
Talbot effect

$$L_{\pi} = \frac{\lambda}{2(n_1 - n_2)} \approx \frac{4n_c W^2}{3\lambda}$$

William Henry Fox Talbot, 1800 – 1877, an English scientist and photography pioneer.

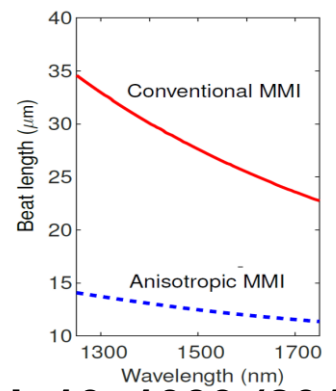
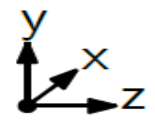


Uniaxial crystal



$$n_{core} = \begin{pmatrix} n_{xx} & 0 \\ 0 & n_{zz} \end{pmatrix}$$

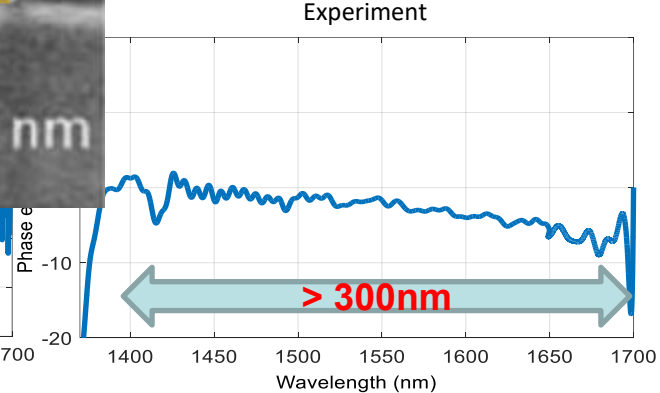
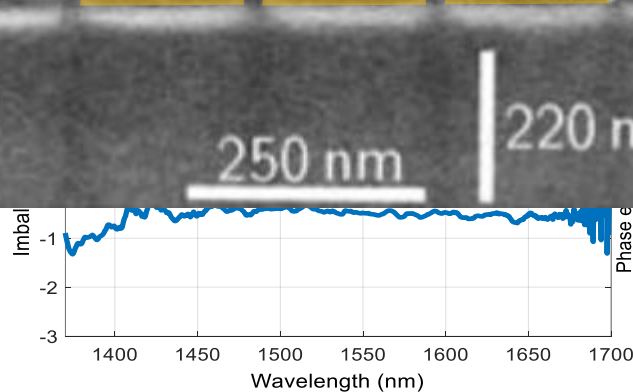
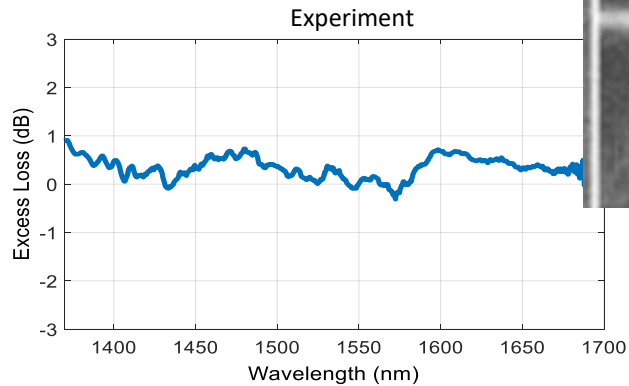
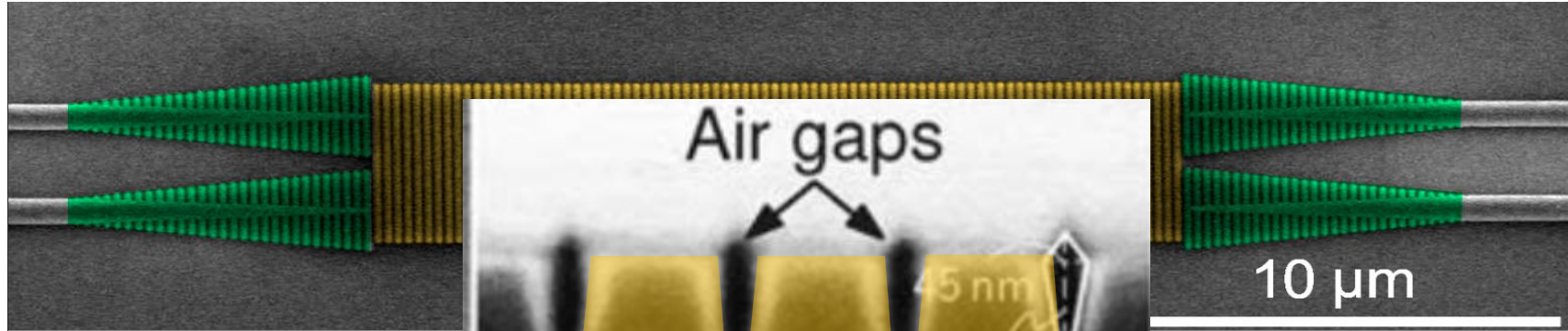
$$L_{\pi}^{aniso} \approx \frac{4W^2}{3\lambda} \frac{n_{zz}^2}{n_{xx}}$$



R. Halir, et al., Laser Photonics Rev., vol. 10, 1039 (2016)

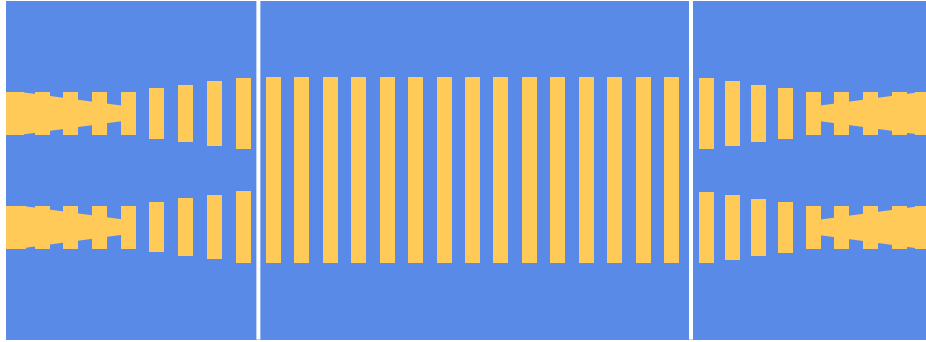
500 nm design bandwidth exceeding all optical communication bands combined

Ultra-broadband MMI (experiment)

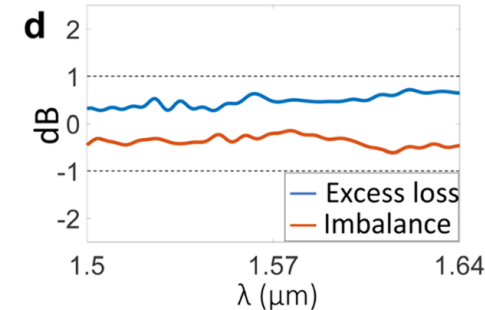
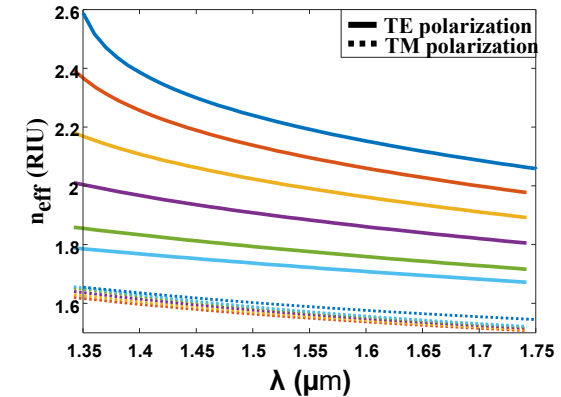
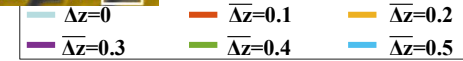
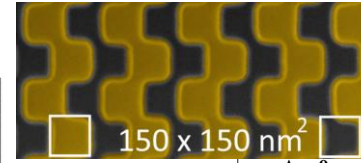
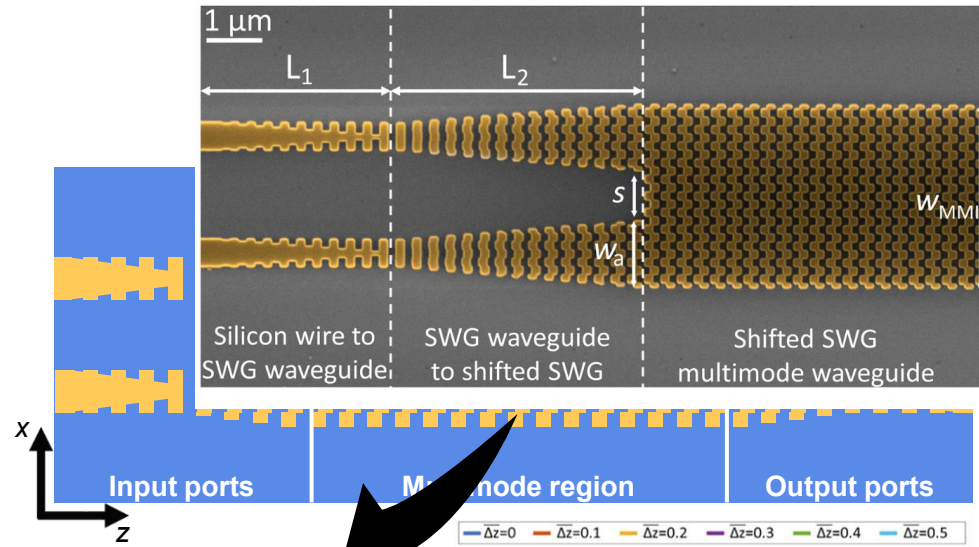


Over 300 nm bandwidth

Ultra-broadband MMI – Uniaxial SWG

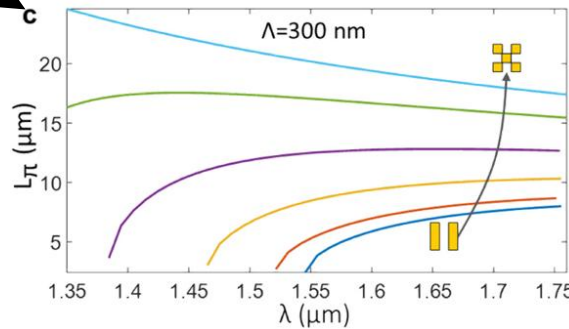


Ultra-broadband MMI - Biaxial SWG

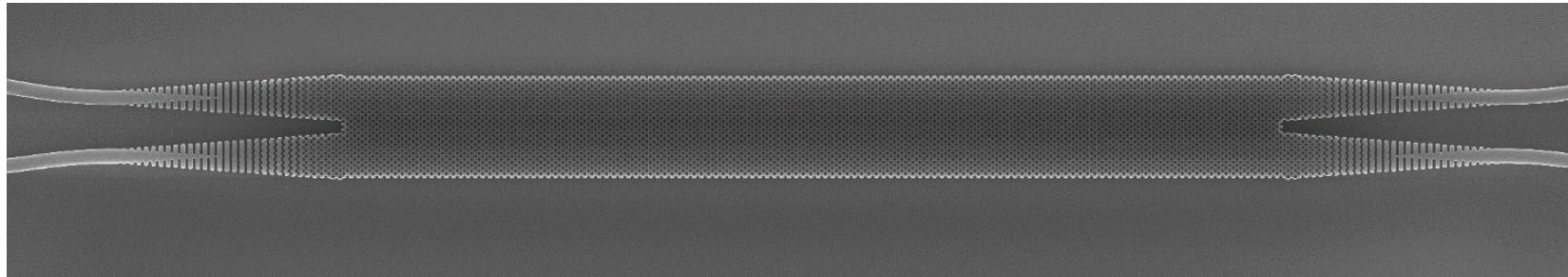
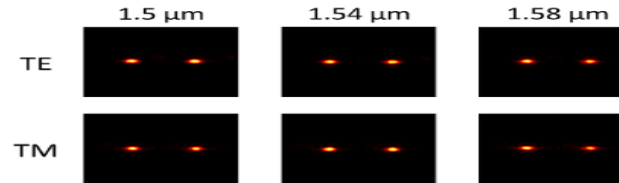
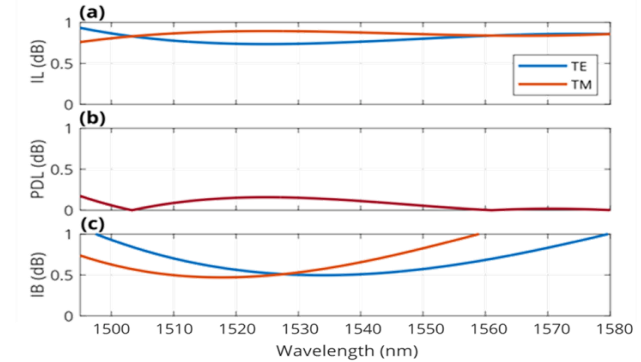
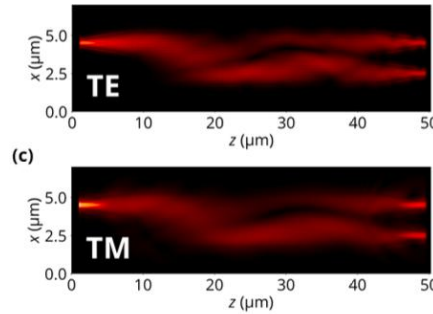
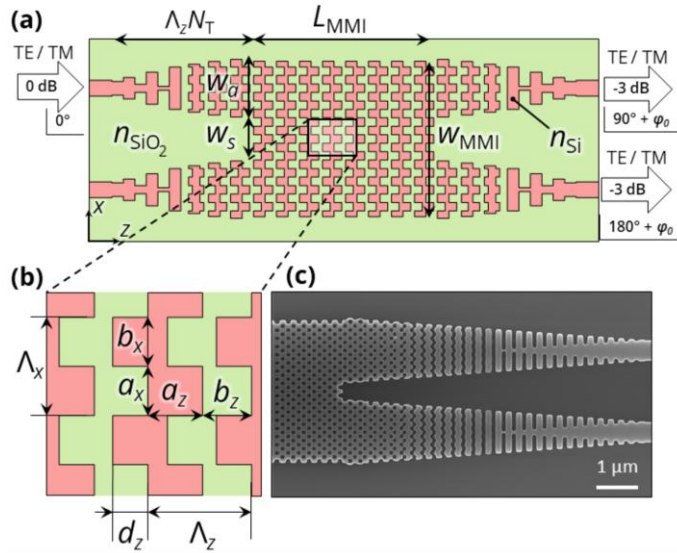


$$\begin{bmatrix} n_{xx}^2 & 0 & 0 \\ 0 & n_{yy}^2 & 0 \\ 0 & 0 & n_{zz}^2 \end{bmatrix}$$

$$L_{\text{mmi}} \propto \frac{W^2 n_{zz}^2(\lambda)}{\lambda n_{xx}(\lambda)}$$



Polarization independent MMI



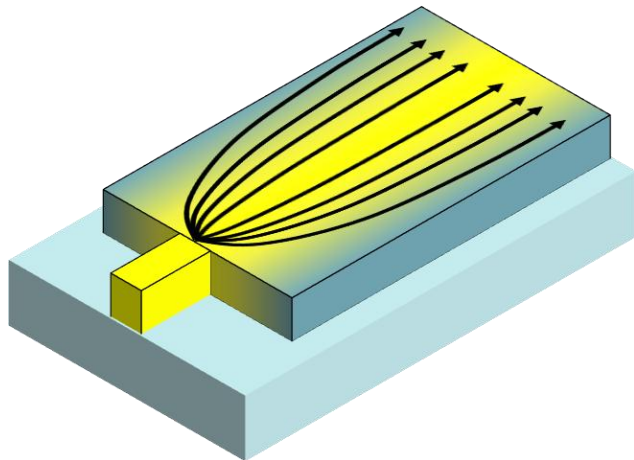
C. Pérez-Armenta, et al., "Polarization insensitive metamaterial engineered multimode interference coupler in a 220 nm silicon-on-insulator platform" 2023

Graded index metamaterial

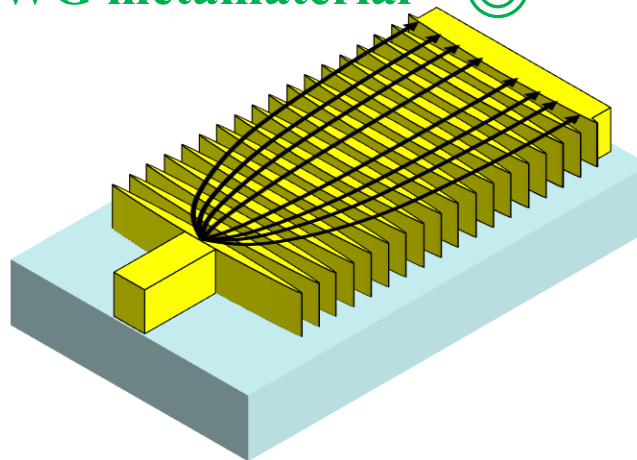
Expanding the beam

GRIN lens

Beam collimator



SWG metamaterial



An Ultracompact GRIN-Lens-Based Spot Size Converter using Subwavelength Grating Metamaterials

José Manuel Luque-González, Robert Halir, Juan Gonzalo Wangüemert-Pérez, José de-Oliva-Rubio, Jens H. Schmid, Pavel Cheben, Íñigo Molina-Fernández, and Alejandro Ortega-Moñux*

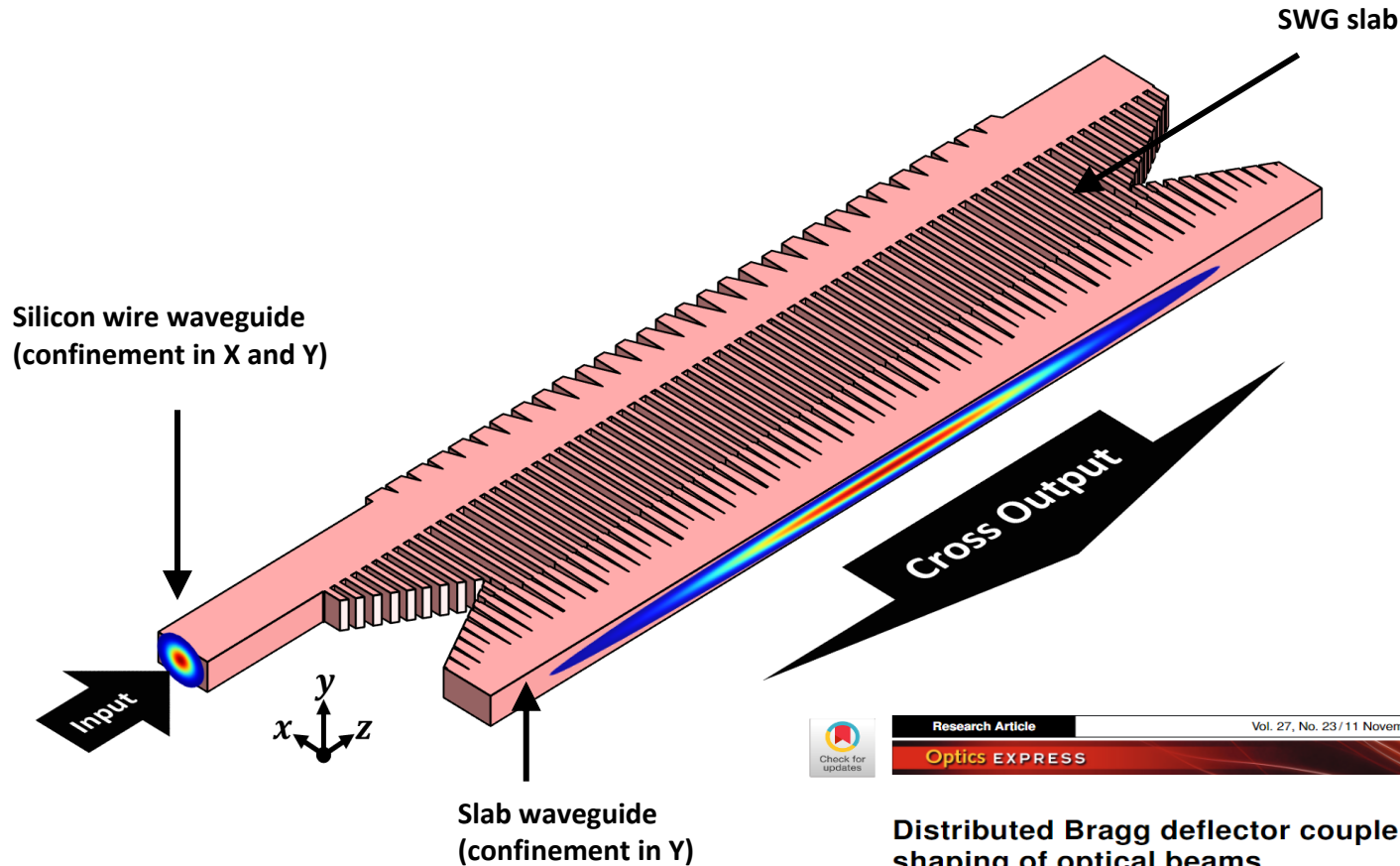
**Beam expansion $0.5 \mu\text{m} \rightarrow 15 \mu\text{m}$
in $14 \mu\text{m}$**

< 0.6 dB losses

**Same losses & BW as
 $150 \mu\text{m}$ long taper**



Courtesy - Prof. Inigo Molina Fernandez



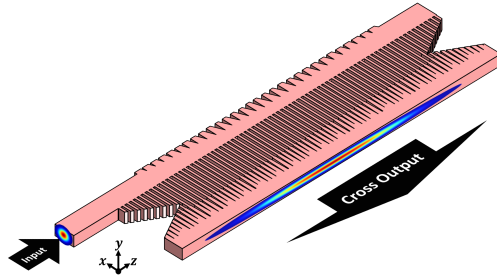
Research Article

Vol. 27, No. 23/11 November 2019 / Optics Express 33180

Optics EXPRESS

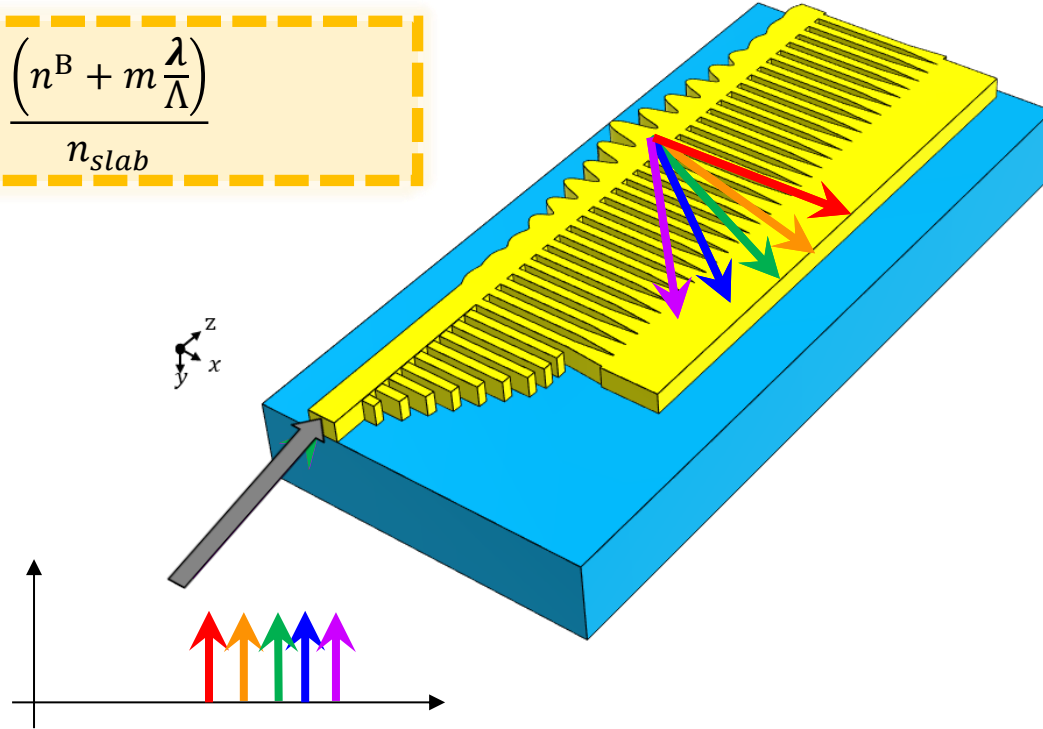
Distributed Bragg deflector coupler for on-chip shaping of optical beams

ABDELFETTAH HADIJ-ELHOUATI,^{1,*}  PAVEL CHEBEN,³ 
ALEJANDRO ORTEGA-MOÑUX,¹ J. GONZALO
WANGÜEMERT-PÉREZ,¹  ROBERT HALIR,^{1,2} JENS H. SCHMID,³
AND ÍÑIGO MOLINA-FERNÁNDEZ^{1,2} 



Wavelength steering

$$\sin(\theta) = \frac{\left(n^B + m \frac{\lambda}{\Lambda}\right)}{n_{slab}}$$

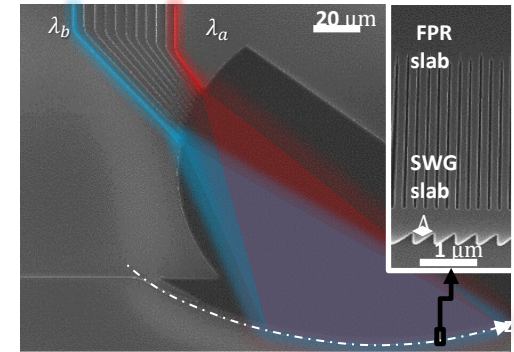
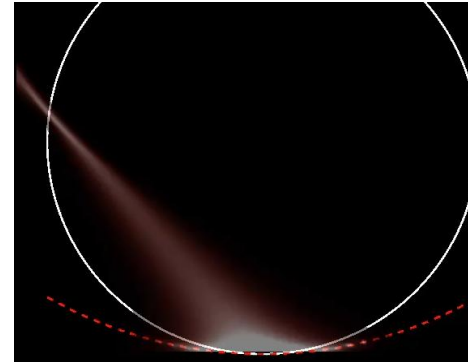
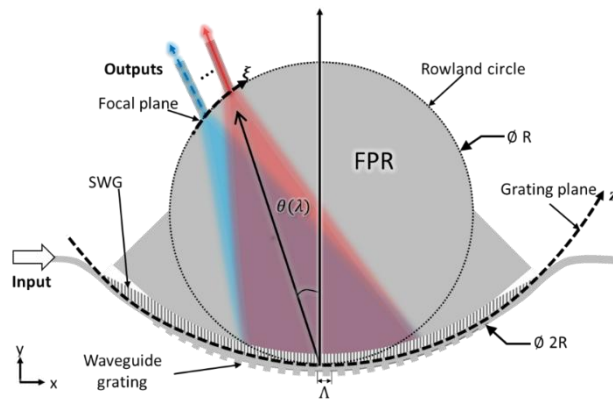


Low-loss wavelength demultiplexer

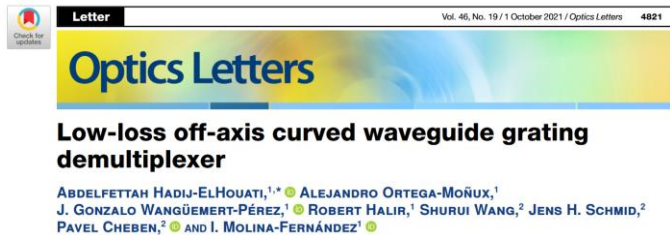
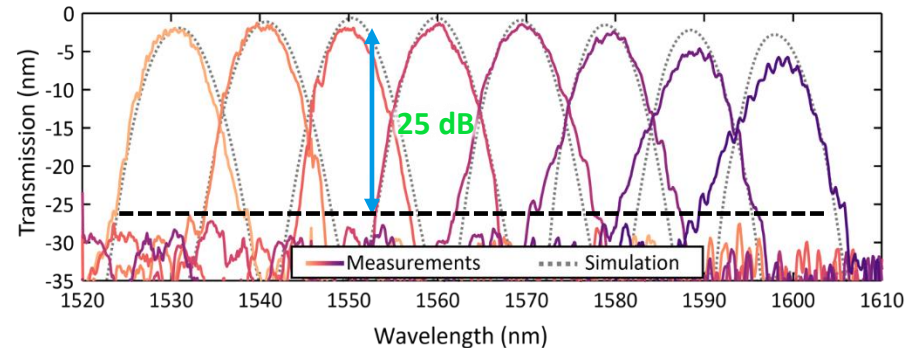
A.H. Elhouati, Opt. Lett. 46, 2409-2412 (2021)

TOP DOWNLOADS

EDITORS' PICK



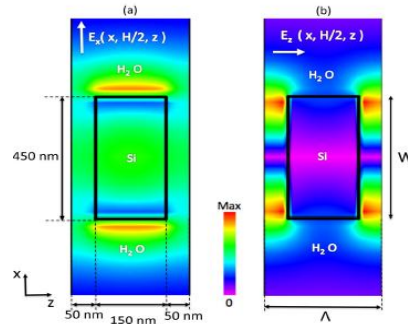
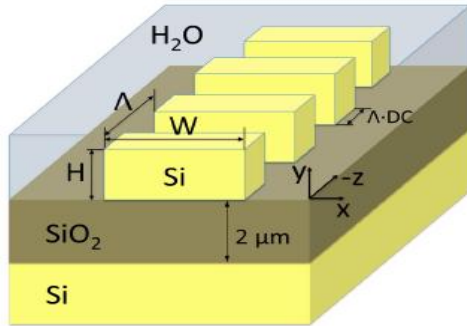
Insertion Loss 1.1 dB
Crosstalk < -25 dB



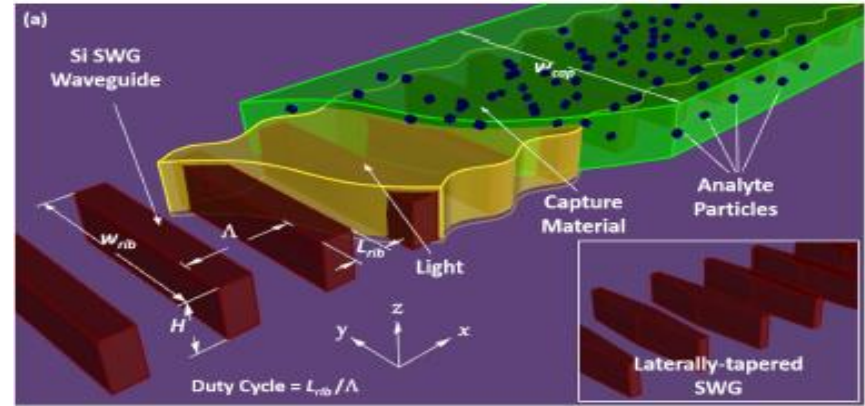
Courtesy - Prof. Inigo Molina Fernandez

SWG waveguides for biochemical sensing

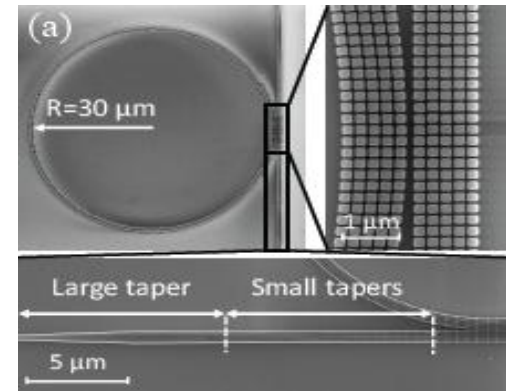
G. Wangüemert-Pérez *et al.*,
Opt. Lett. 39, 4442 (2014)



**Gaps allow increased interaction of
analyte molecules with the waveguide
mode**

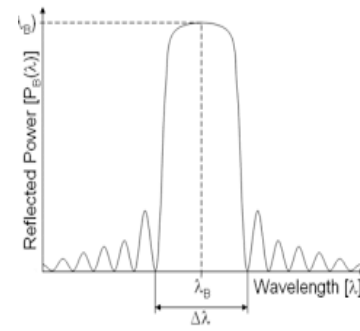
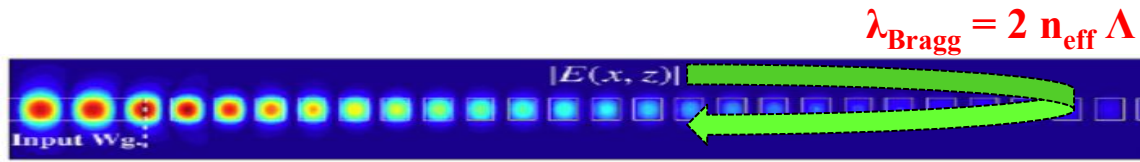


US Army Research Lab
J. Bickford *et al.*, JSTQE vol. 25, no. 3 (2019)



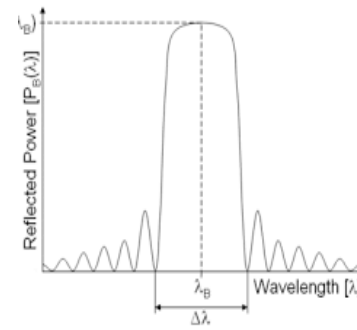
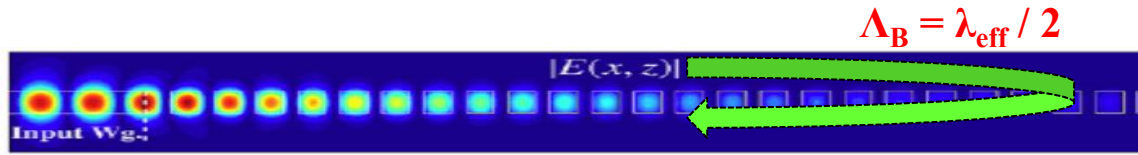
Univ. of British Columbia and Washington Univ.
J. Flueckiger *et al.*, Optics Express (2015)

Waveguide Bragg gratings



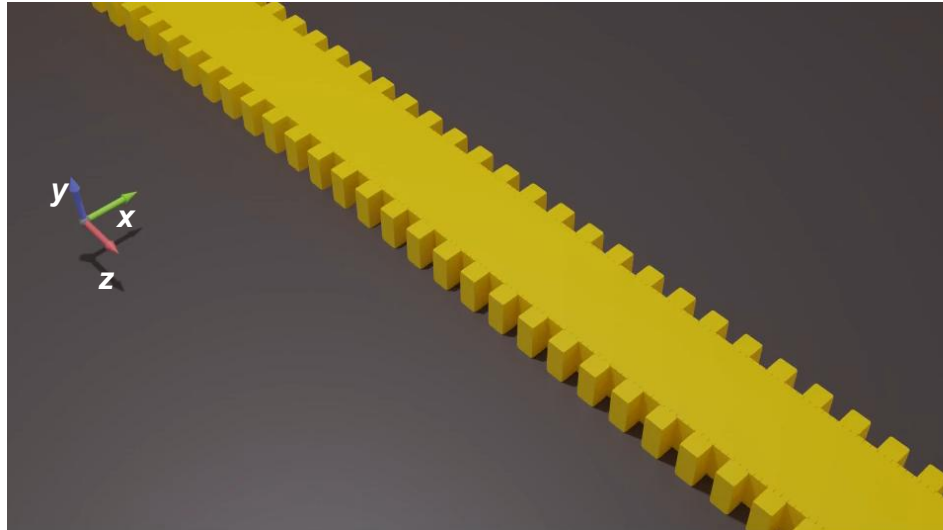
$$\Delta\lambda = \frac{\lambda_0^2}{\pi n_g} \sqrt{k^2 + \left(\frac{\pi}{L_F}\right)^2}$$

Waveguide Bragg gratings



$$\Delta\lambda = \frac{\lambda_0^2}{\pi n_g} \sqrt{k^2 + \left(\frac{\pi}{L_F}\right)^2}$$

- In silicon waveguides, high Δn makes it difficult to accurately control the grating strength and achieve narrow spectral bandwidths.



α

$g(\mu m)$

- SWG engineering can be used to control the bandwidth

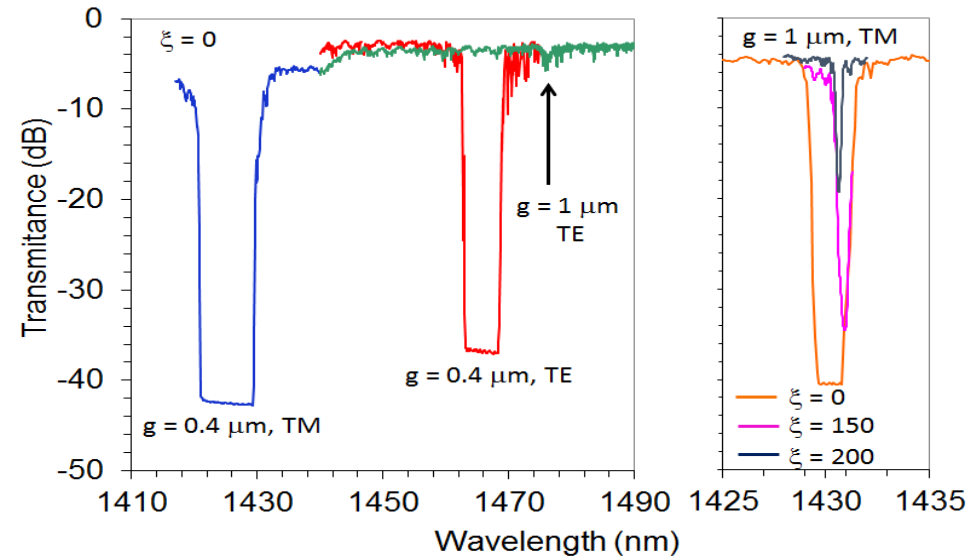
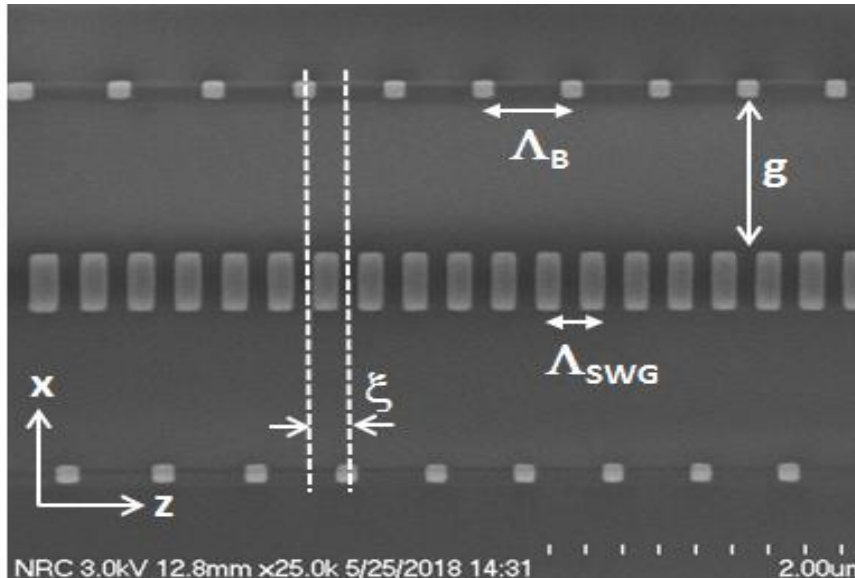
J. Wang et al., Opt. Express 22, 5335 (2014)

D. Oser et al., Opt. Lett. 43, 3208 (2018)

$$k \propto \int |E|^2 \cdot \Delta\epsilon(x, y, z) dV$$

SWG Bragg filters

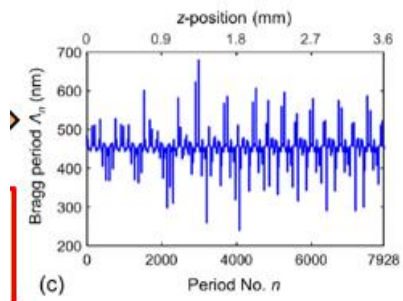
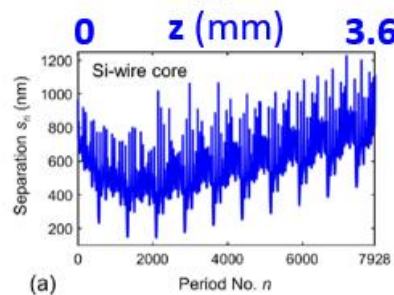
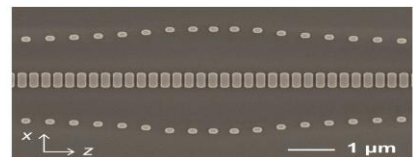
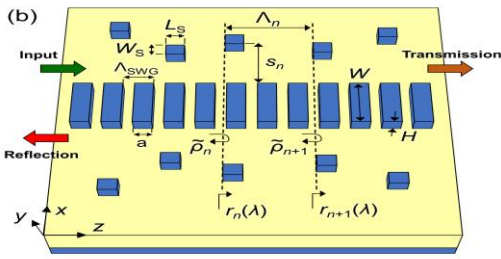
Grating strength controlled by adjusting the gap and the lateral shift



J. Ctyroky et al., Opt. Express 26 (2018)
P. Cheben et al., Optics Letters 44 (2019)

**Filter bandwidth tuned
from 8 nm to 150 pm**

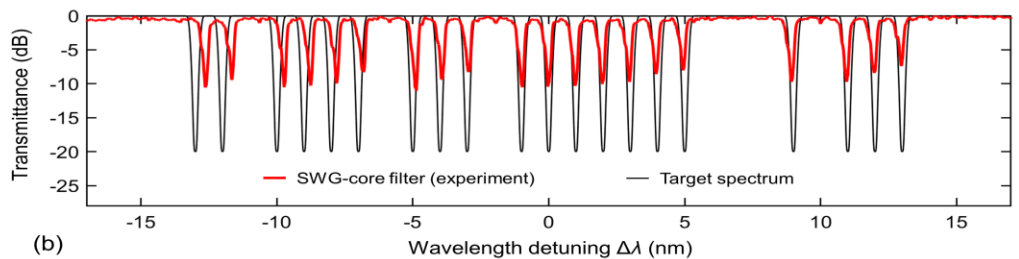
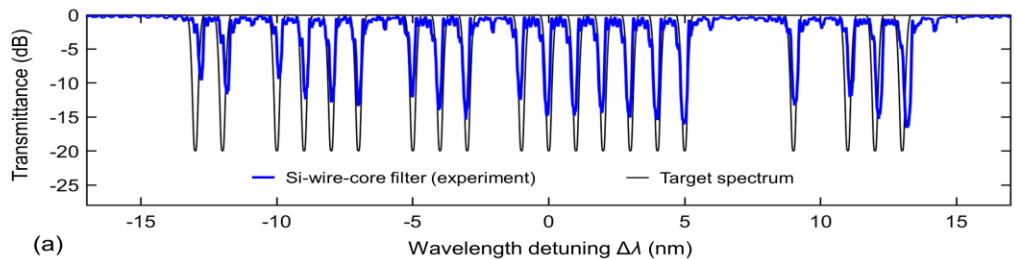
Complex spectral filters



Complex spectral filters in silicon waveguides based on cladding-modulated Bragg gratings

DANIEL PEREIRA-MARTÍN,^{1,*} JOSÉ MANUEL LUQUE-GONZÁLEZ,¹ J. GONZALO WANGÜEMERT-PÉREZ,¹ ABDELFTTAH HADIJ-ELHOUATI,¹ ÍÑIGO MOLINA-FERNÁNDEZ,¹ PAVEL CHEBEN,² JENS H. SCHMID,²

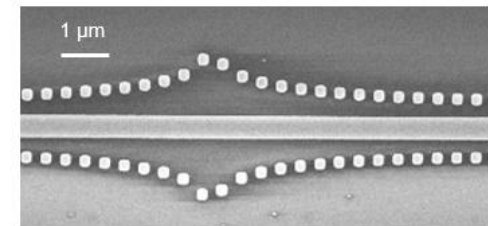
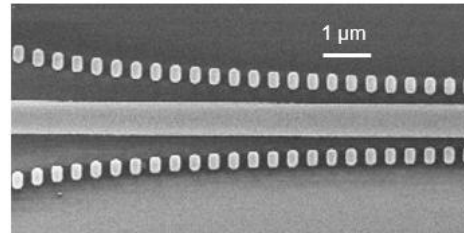
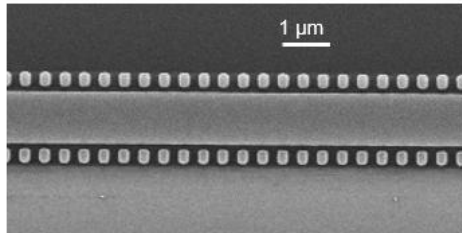
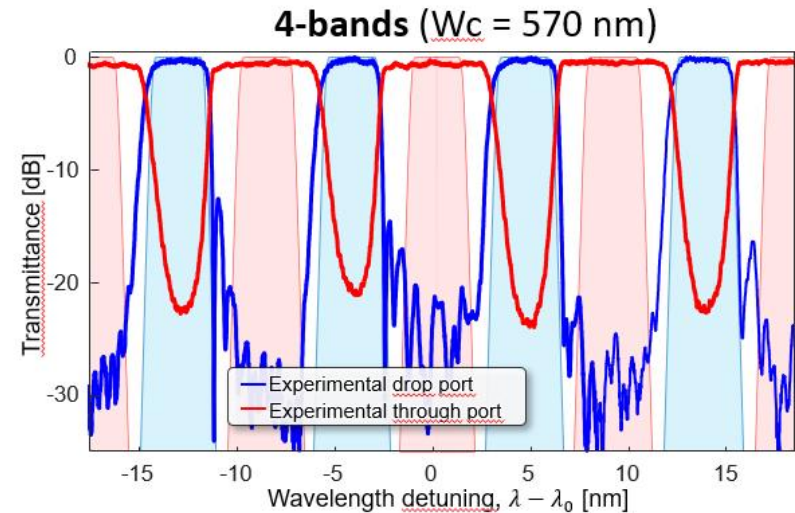
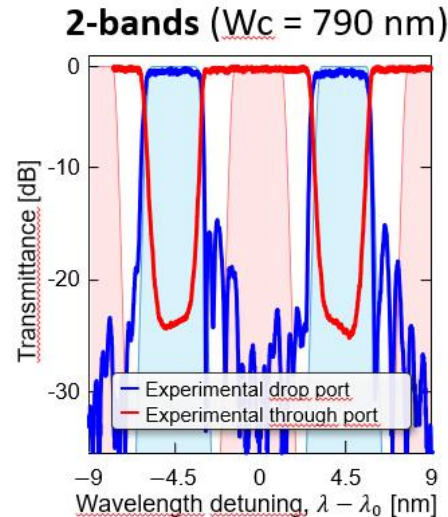
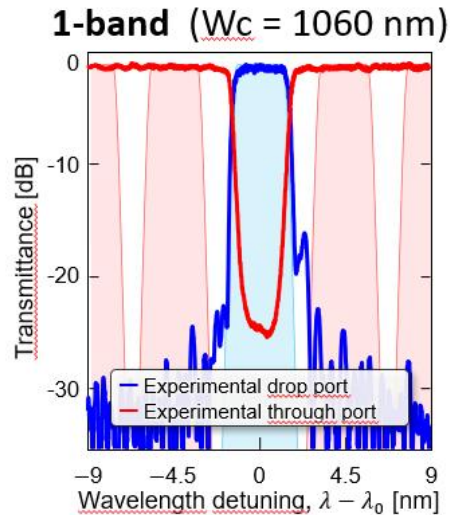
Layer peeling, J. Skaar et al., IEEE JQE 37 (2001)



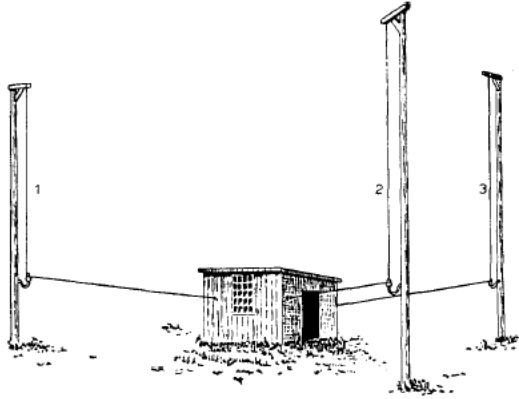
Add-drop filter for LAN-WDM

Experimental results

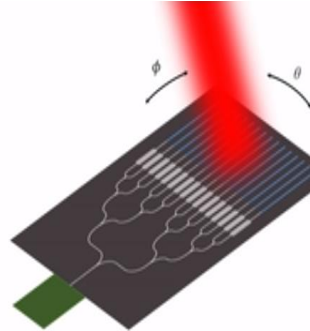
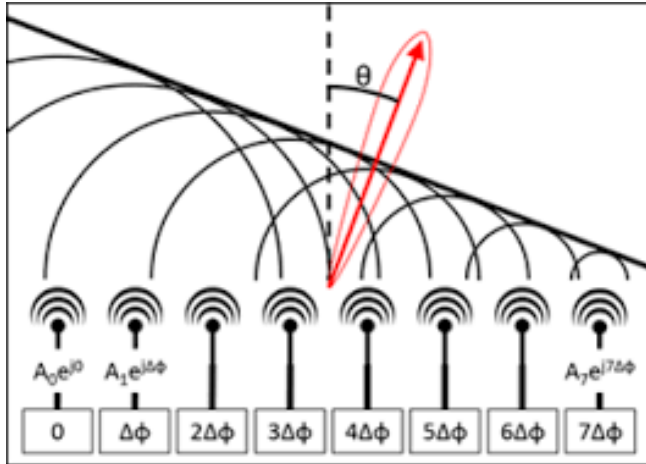
O-band, 1300 nm
Channel spacing 4.5 nm
3dB bandwidth 3 nm
Silicon nitride



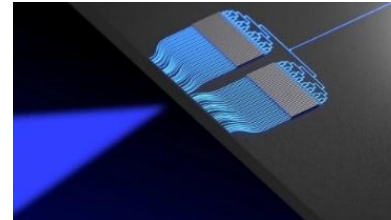
Optical Phased Arrays (OPAs)



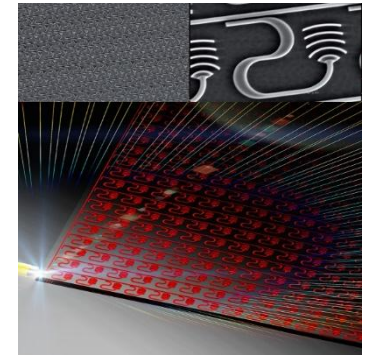
Phased array transmission was originally shown in 1905 by Nobel laureate Karl Ferdinand Braun who demonstrated enhanced transmission of radio waves in one direction.



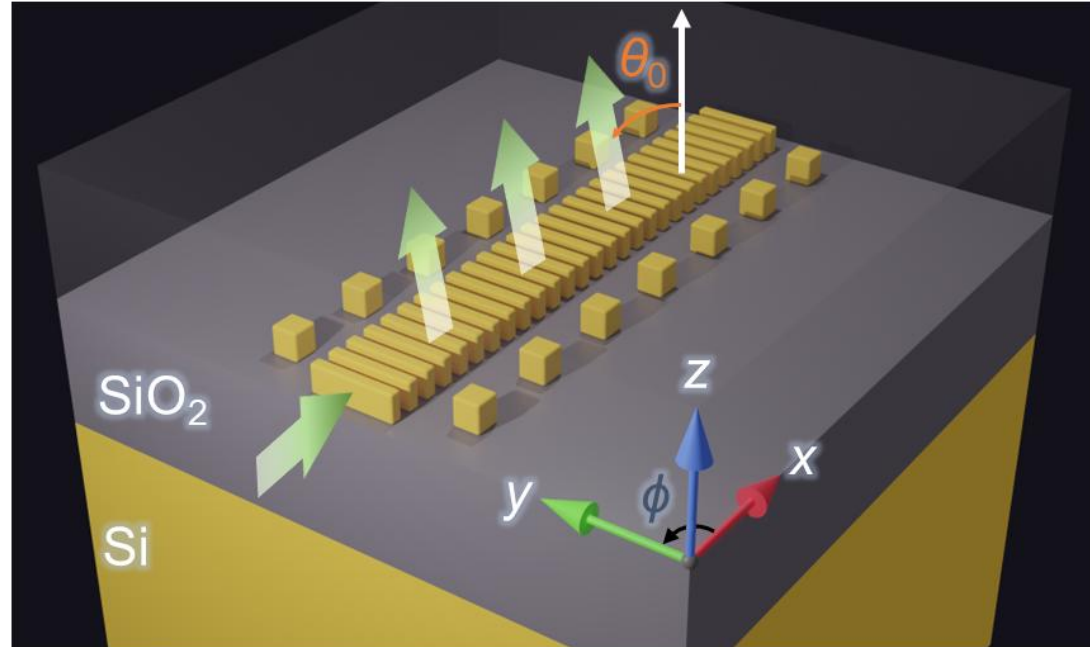
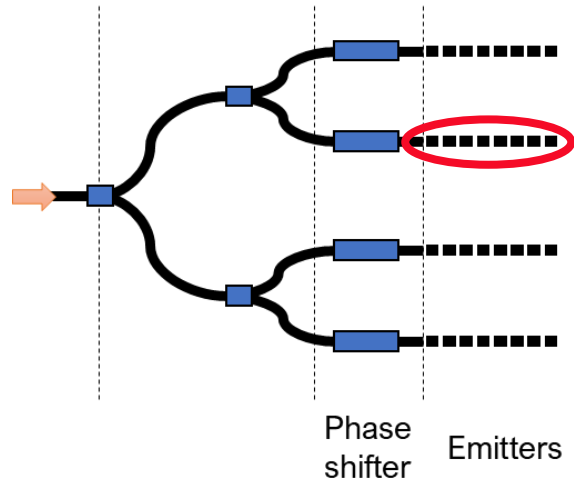
1D OPA



2D OPA

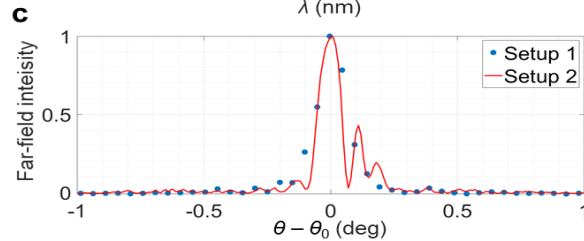
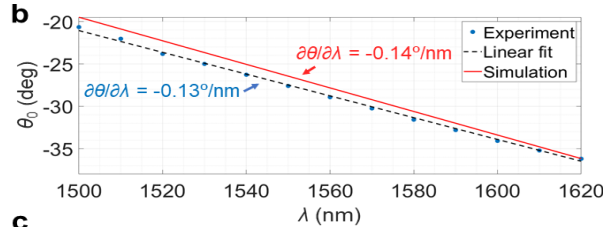
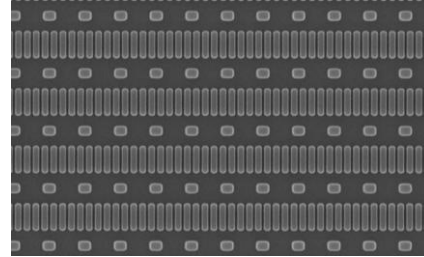
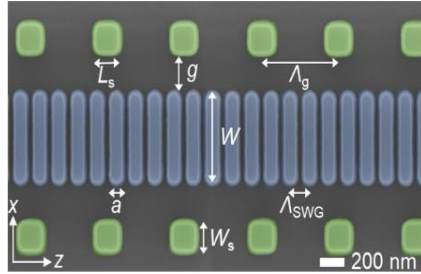


Long waveguide antennas for 1D OPAs



Long waveguide antennas for 1D OPAs

Experimental results



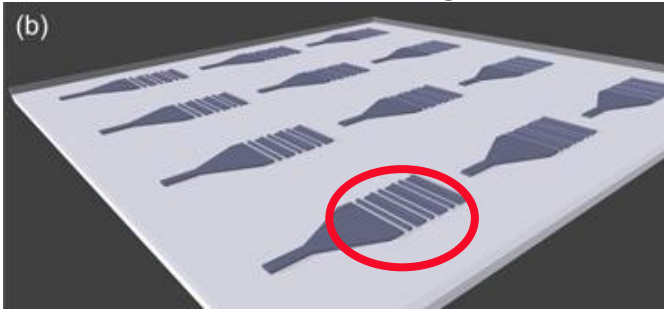
Technology	MFS [nm]	Beam width [deg]	$\partial\theta/\partial\lambda$ [deg/nm]	Ref.
SOI-220nm	80	0.10	0.15	Our work
SOI-220nm	8	0.08	0.26	[1]
SOI-220nm	7	0.15	0.15	[2]
SOI-220nm	7	0.18	0.19	[3]
SOI-500nm	238	0.58	0.14	[4]
Si-SiN	500	0.20	0.07	[5]
Si-SiN	315	0.07	0.17	[6]
Si-SiN	70	0.02	-	[7]

P. Ginel-Moreno et al., Opt. Lett., 2021

P. Ginel-Moreno, Laser Photon. Rev. 16, 2022

Compact grating couplers for 2D OPAs

M x N array



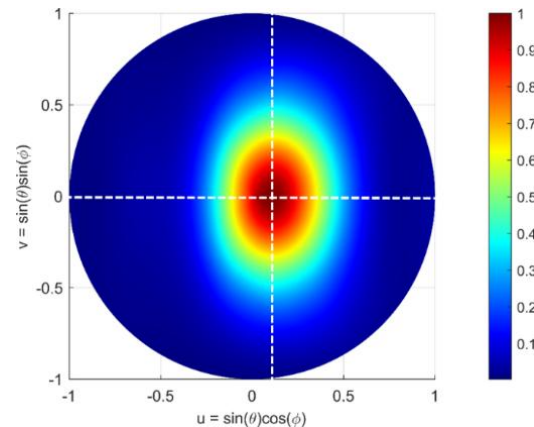
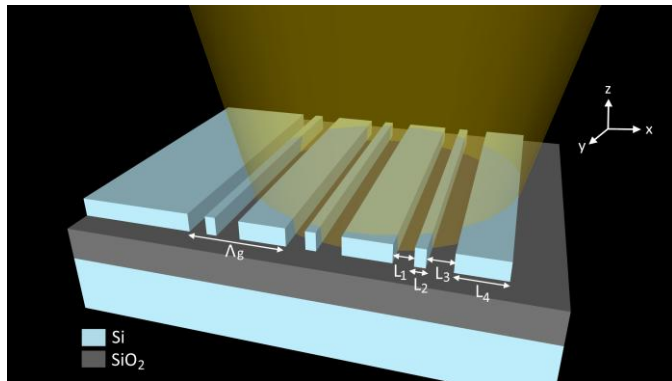
Angular width of far field inversely related to grating aperture size - Fraunhofer transformation.

Angular width determines the maximum steering range of OPA.

So we need short gratings for large steering range, 3-4 periods, but then the efficiency drops

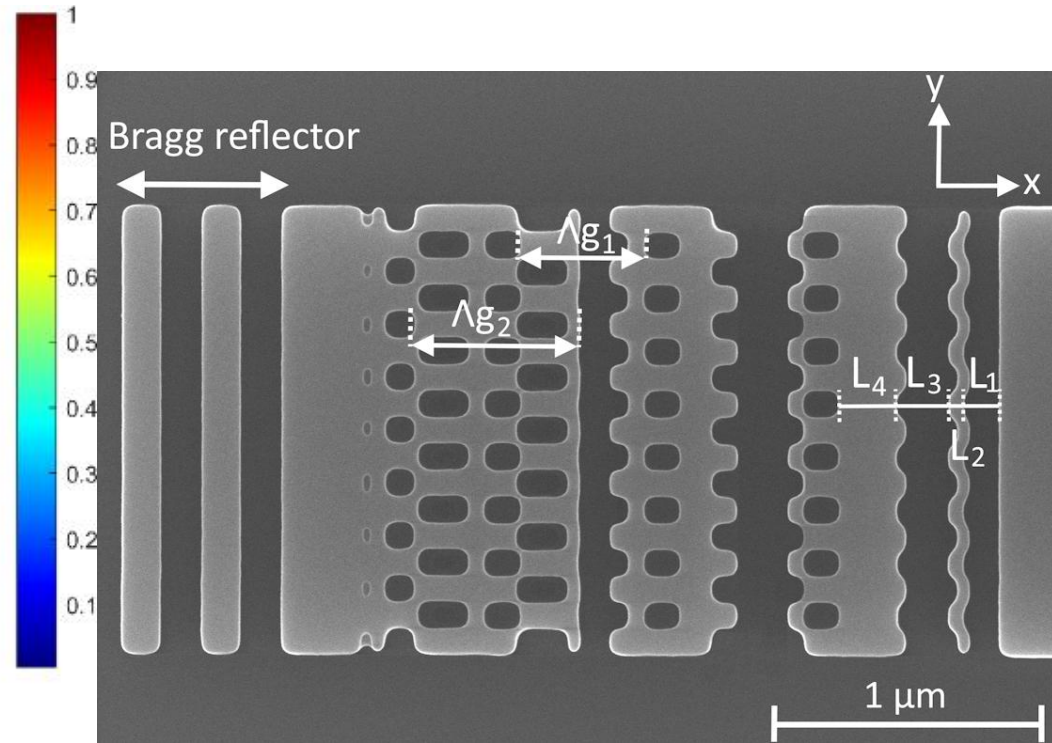
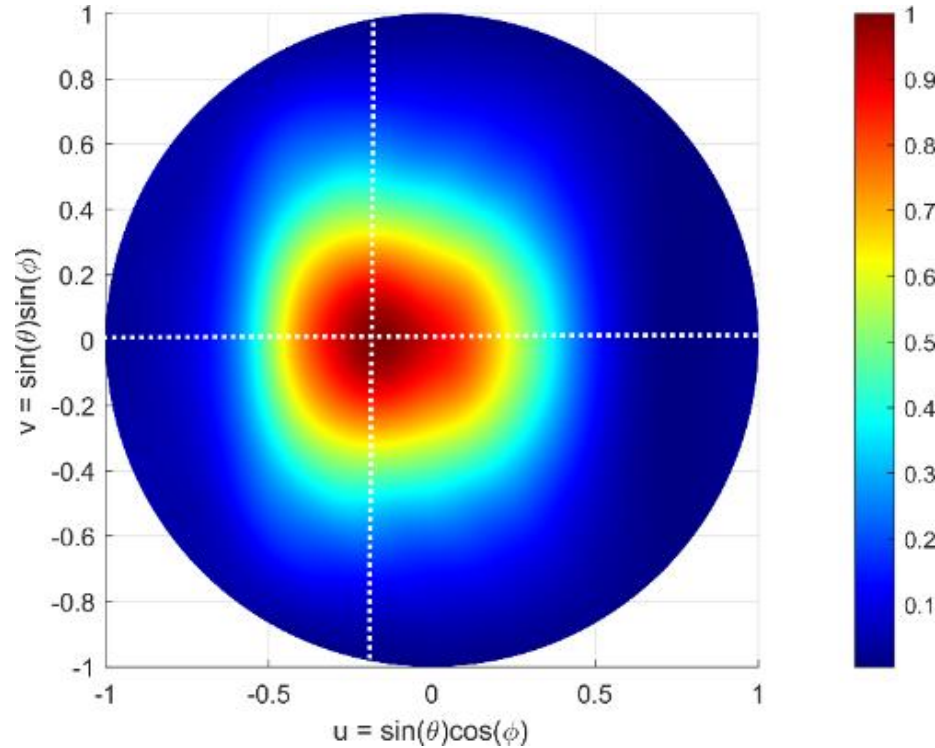
Can we broaden the far field without reducing aperture size?
Beyond Fraunhofer limit?

$$U(x, y, z) \propto \iint_A E(x', y') e^{-i\left(\frac{k(x'x + y'y)}{z}\right)} dx' dy'$$



Far field broadening

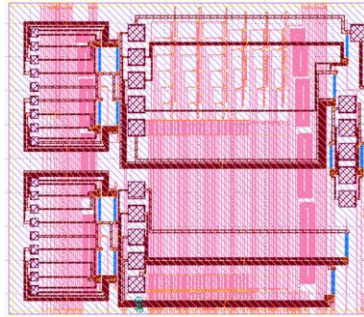
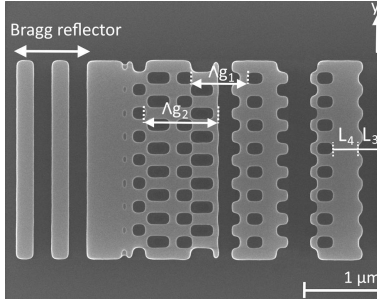
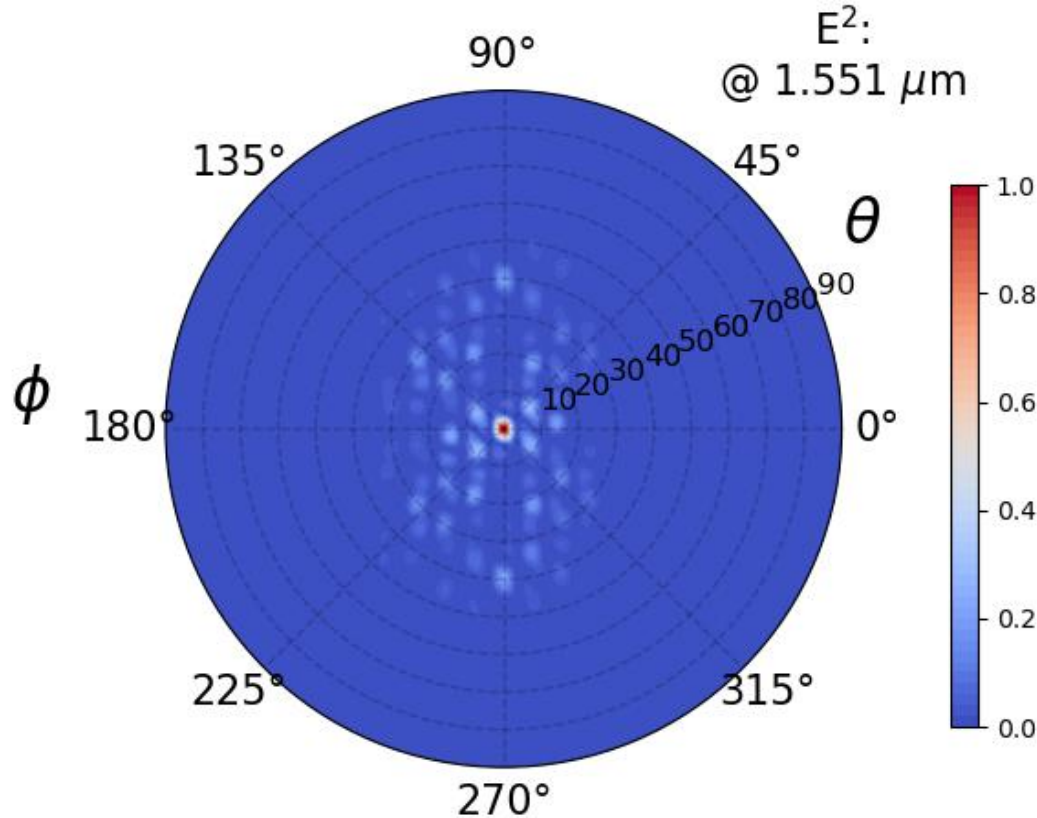
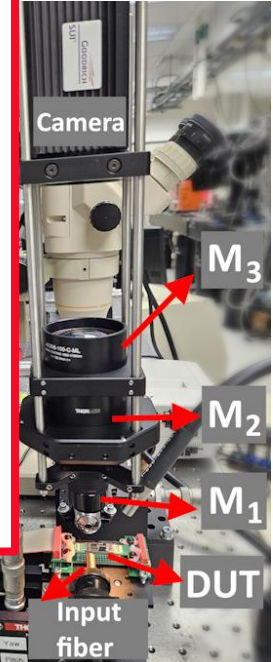
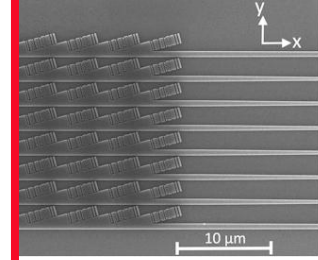
✓ Far-field beam width: $51^\circ \times 47^\circ$



S. Khajavi *et al.*, “Highly efficient ultra-broad beam silicon nanophotonic antenna based on near-field phase engineering”, *Sci. Rep.*, 12, 1–8, (2022).

Larger scale array

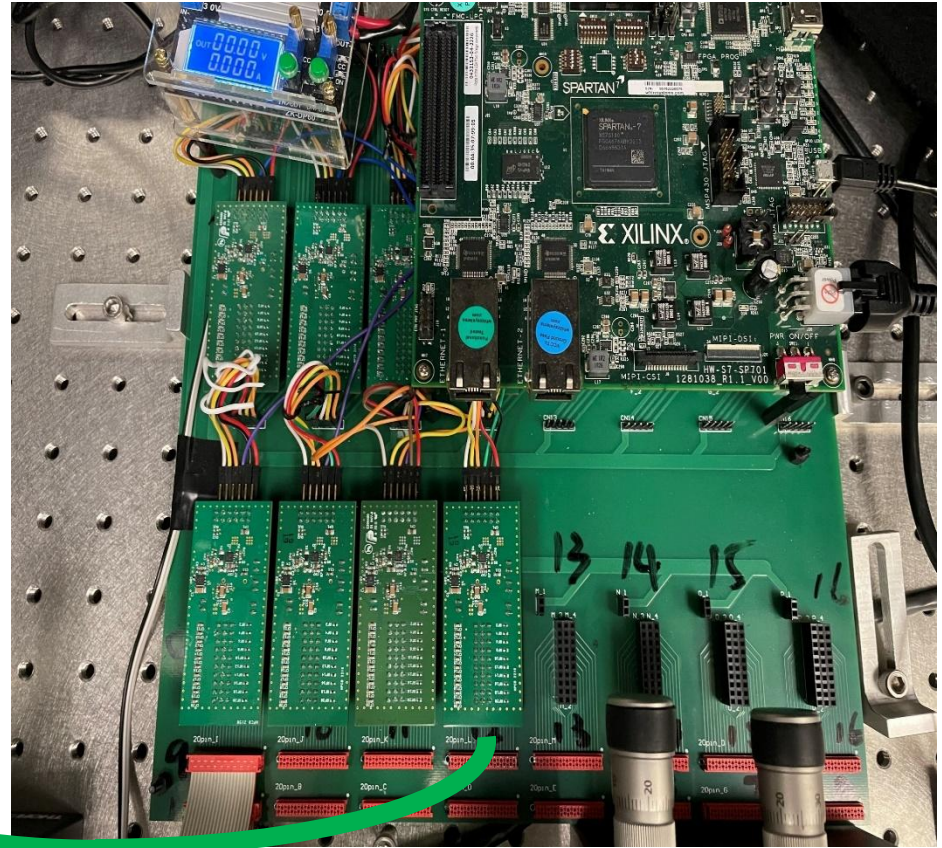
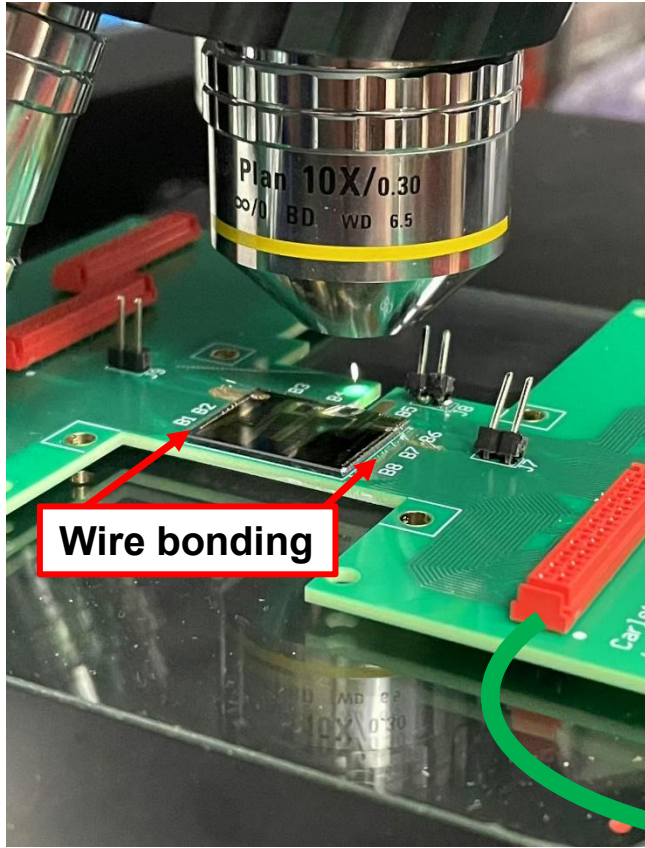
8×20 array



300-nm Si core, 21×
TO Phase shifters:

S. Khajavi *et al.*, “E
nanophotonic antenna for far-field broadened optical
phased arrays”, *Photonics Research*, 2024.

Hardware and control interface



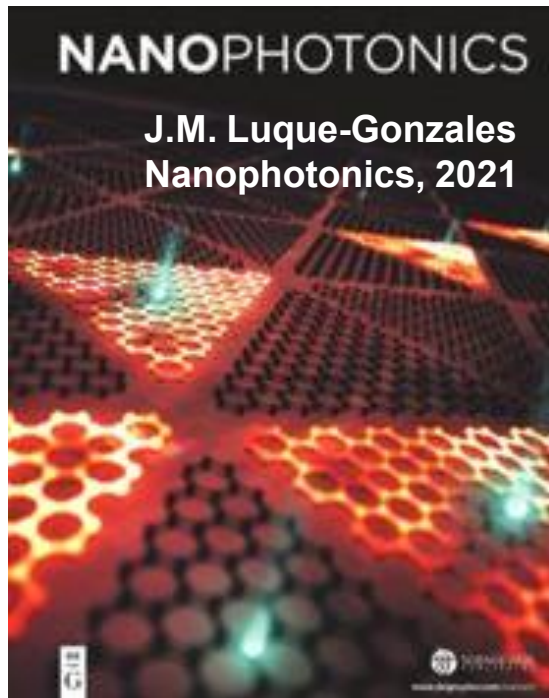
Cable connection between PCB and FPGA

Review Article | Published: 29 August 2018

Subwavelength integrated photonics

Pavel Cheben , Robert Halir, Jens H. Schmid, Harry A. Atwater & David R. Smith

Nature **560**, 565–572 (2018) | [Download Citation](#) 



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Recent advances in metamaterial integrated photonics

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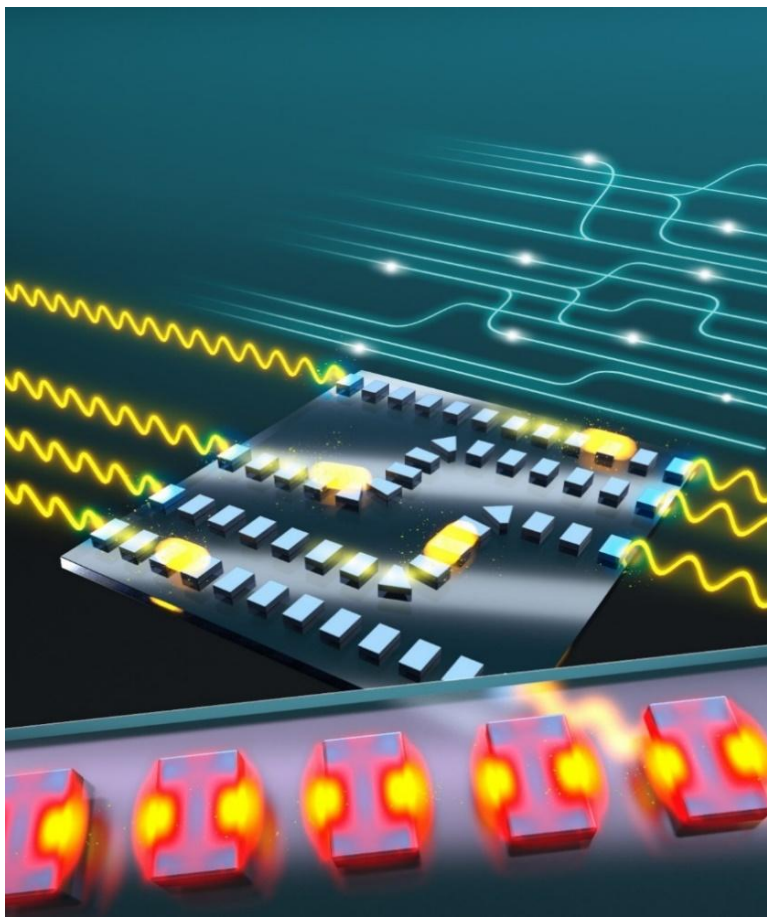
P. Cheben et al., Nature 560, p. 565, 2018

R. Halir et al., Proceedings of the IEEE, 2018

J.M. Luque-Gonzales, Nanophotonics, 2021

P. Cheben et al., Advances in Optics and Photonics, 2023

<https://doi.org/10.1364/AOP.495828>



Děkuji

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